

Hopko

FEB 3 1947 547

PTD-EA

NATIONAL ADVISORY COMMITTEE
FOR AERONAUTICS

TECHNICAL NOTE

No. 1200

TENTATIVE TABLES FOR THE PROPERTIES
OF THE UPPER ATMOSPHERE

By Calvin N. Warfield

for the

NACA Special Subcommittee on the Upper Atmosphere

Langley Memorial Aeronautical Laboratory
Langley Field, Va.



Washington

January, 1947

M
NACA LIBRARY
LANGLEY MEMORIAL AERONAUTICAL
LABORATORY

Langley Field, Va.



3 1176 01433 9015

NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

TECHNICAL NOTE NO. 1200

TENTATIVE TABLES FOR THE PROPERTIES
OF THE UPPER ATMOSPHERE

By Calvin N. Warfield

for the

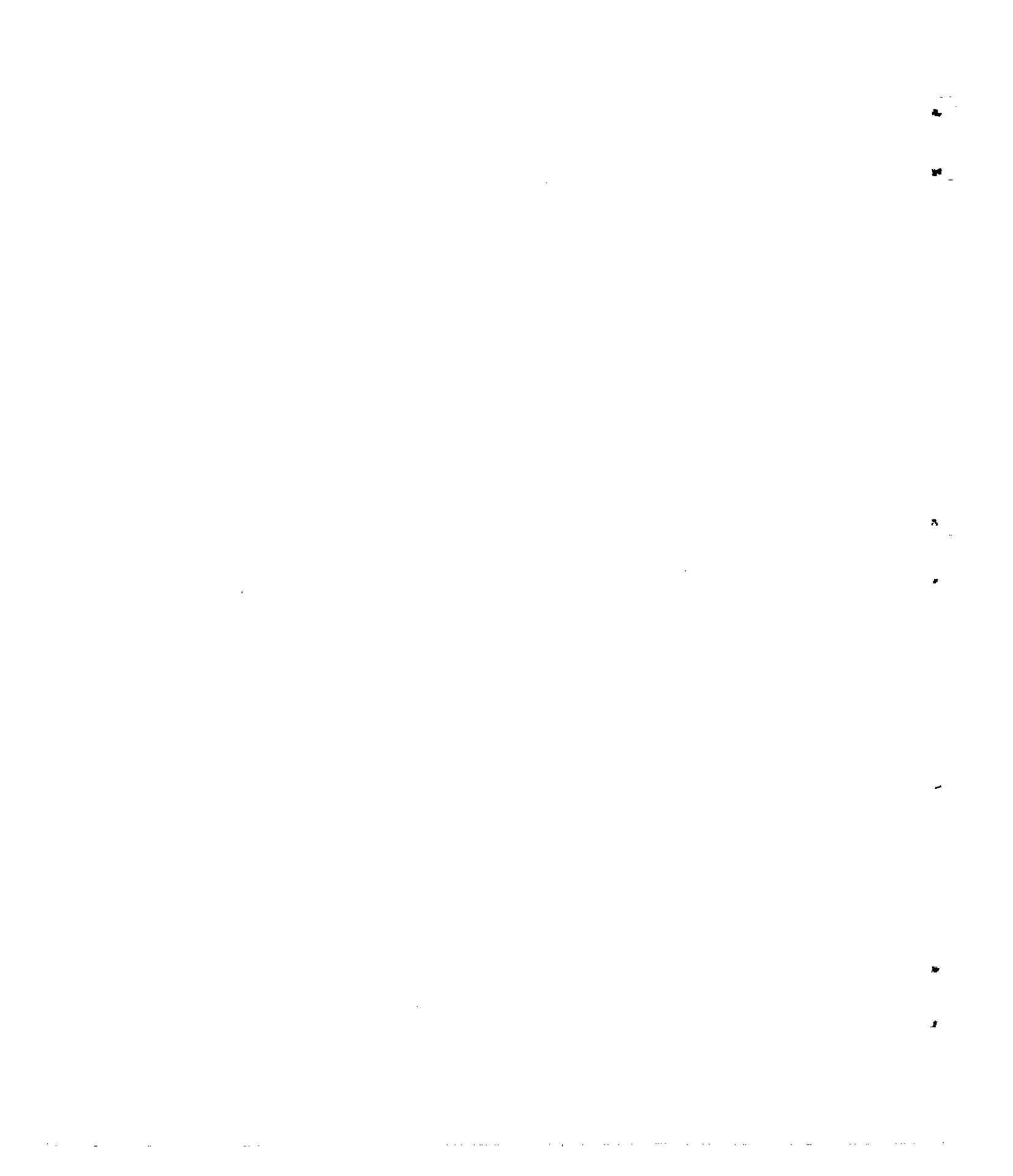
NACA Special Subcommittee on the Upper Atmosphere

SUMMARY

As a result of recent developments in aeronautics and ordnance, a need has arisen for tables of properties of the atmosphere at altitudes in excess of those covered by the existing standard tables (NACA Report No. 218). In order to satisfy this need, the National Advisory Committee for Aeronautics has adopted three temperature-height relationships and one composition-height relationship, and tables based upon them have been prepared for pertinent properties of the upper atmosphere (that is, from 20 to 120 kilometers in metric units, and from 65,000 to 393,700 feet in British units). In the absence of direct data, such as might be obtained by soundings with high-altitude rockets, the values adopted are based upon existing information obtained by indirect measurements of certain quantities. As a consequence, the tables are only tentative.

Two sets of tables based upon the adopted tentative standard specifications for the upper atmosphere are presented. One set of two tables is based upon the same arbitrary constant value for the acceleration of gravity as was used in the preparation of the existing standard tables for the lower levels (NACA Report No. 218). This set of tables for the upper levels of the atmosphere therefore constitutes a consistent extension of the existing standard tables. The other set of two tables takes into consideration the decrease in the acceleration of gravity with increasing altitude and therefore is more precise than the first set. Consequently, this set is presented only to satisfy the need for greater accuracy that may exist in some fields of research.

Each table is divided into separate parts for both day and night conditions at altitudes above 80 kilometers. The necessity for separate tables for day and night values is occasioned by the



In April 1946 this Panel was superseded by the Special Subcommittee on the Upper Atmosphere which was also appointed by the NACA.

The membership of this Special Subcommittee is as follows:

*Dr. Harry Hall - Harry E. T.
Dr. Joseph Kaplan, C.I.T.*

Dr. Harry Wexler, U. S. Weather Bureau, Chairman

Col. D. N. Yates, Chief, Air Weather Service

Col. Paul H. Dane, A. C., TSEAC, AAF Air Materiel Command

Capt. H. T. Orville, USN, Office of Chief of Naval Operations,
Navy Department

Capt. Walter S. Diehl, USN, Bureau of Aeronautics, Navy
Department

^.-Dr. Calvin N. Warfield, Langley Memorial Aeronautical Laboratory

Dr. E. H. Krause, Naval Research Laboratory

Dr. W. G. Brrombacher, National Bureau of Standards

Dr. L. V. Berkner, Carnegie Institution of Washington

Dr. B. Gutenberg, California Institute of Technology

Dr. Fred L. Whipple, Harvard Observatory, Harvard University

Dr. O. R. Wulf, Gates and Crellin Laboratories, California
Institute of Technology.

Mr. Jerome Teplitz, NACA, Secretary.

This Subcommittee has considered the information available concerning temperature and composition in the upper atmosphere. On the basis of existing data obtained by balloons at altitudes up to about 32 kilometers (references 6 and 7), of indirect measurements obtained at greater heights such as those discussed in references 8 to 14, and of unpublished data resulting from similar indirect measurements, recommendations concerning temperature-height and composition-height relationships were made by the Subcommittee on June 24, 1946. The recommendations regarding temperature-height relationships cover three arbitrary sets of temperature: (1) tentative standard temperatures, (2) probable minimum temperatures, and (3) probable maximum temperatures. Also, recommendation was made that at this time no tables be prepared for altitudes in excess of 120 kilometers because of the uncertainty regarding the validity of the data in this region.

At a meeting of the executive committee of the National Advisory Committee for Aeronautics held on August 15, 1946, the previously mentioned recommendations of the Subcommittee were adopted. As a result of the adoption of the recommendations of the Subcommittee, two sets of tables for the upper atmosphere, based upon the tentative standard temperatures, have been prepared at the Langley Laboratory of the NACA.

The first set of tables provides a consistent extension of the present standard tables for the lower levels of the atmosphere

(reference 1) because the same simplifying assumption of an arbitrary constant value for the acceleration of gravity is made in both cases. Because of this consistency with the present standard atmosphere tables, and in consideration of the fact that the present standard tables (reference 1) are widely used in evaluating performance characteristics of aircraft and for design purposes, it appears that this first set of tables may also be found useful in these same fields of aeronautical engineering. In addition, in order to be consistent with present practice in the use of the terms "pressure altitude" and "density altitude" (reference 15) it appears that it may be proper to use the term "tentative pressure altitude" to designate that altitude in this first set of tables which corresponds to a specified ambient-air pressure. Likewise, the term "tentative density altitude" can consistently be used with this set of tables in connection with ambient-air densities.

The second set of tables is more precise than the first because it takes into consideration the decrease in the acceleration of gravity with increasing altitude. This set is intended primarily for use in connection with research on the properties of the upper atmosphere. Values of still greater computational precision than those listed in this second set may be obtained by means of "latitude correction factors" which have been computed and tabulated in another table.

These two sets of tables for the upper atmosphere consist of two tables each, one in the metric system of units and the other in the British system of units. The altitude range covered is from 20 kilometers and 65,000 feet, respectively, to 120 kilometers and its British equivalent of about 393,700 feet. In addition to those quantities reported in references 1 to 5, there is included the mean free path of the air molecules. This quantity has been added because of its significance at high altitudes where the molecular mean free paths may be comparable to or larger than certain dimensions of the aircraft or missiles that may be flown there.

Acknowledgement is gratefully given for the contributions made by Dr. R. G. Stone, of the AAF Weather Service, who supplied valuable data concerning maximum and minimum temperatures over the entire world to altitudes of 32 kilometers, and for the thorough technical review and excellent suggestions offered by Mr. L. P. Harrison of the U. S. Weather Bureau.

SYMBOLS

a	speed of sound
c	most probable molecular speed
\bar{c}	average molecular speed
g	acceleration of gravity
h	altitude
K	volume gradient of oxygen dissociation $\left(\frac{\Delta v}{\Delta h} \right)$
L	temperature gradient $\left(\frac{\Delta T}{\Delta h} \right)$
M	molecular weight
m	mass of a molecule
N	number of molecules per unit volume
p	pressure
R	universal gas constant
r	radius of the earth
T	absolute temperature
t	temperature
v	volume of molecular oxygen in an initial unit volume of normal air, at the same temperature and pressure
w	specific weight (g_0)
γ	ratio of specific heats

- λ mean free path of molecules
 μ coefficient of viscosity
 ν kinematic viscosity (μ/ρ)
 ρ density (mass per unit volume)
 σ molecular diameter; also density ratio (ρ/ρ_0)
 $\bar{\sigma}$ average molecular diameter

The following subscripts are used to refer to the indicated conditions:

- 0 sea level
1 lower level
a top of region of dissociation, where oxygen is all atomic
A base of region with constant temperature and constant composition
B base of region with constant temperature gradient and constant composition
C base of region with constant temperature and constant volume gradient of dissociation
D base of region with constant temperature gradient and constant volume gradient of dissociation
g acceleration of gravity variable
m base of region of dissociation, where oxygen is all molecular
n nitrogen molecules
N non-oxygen (i. e., all constituents other than oxygen)
o oxygen
air mixture of molecules in atmosphere
 ϕ latitude

ADOPTED SPECIFICATIONS FOR THE UPPER ATMOSPHERE

Tentative Temperatures

Three sets of tentative temperature-height relationships have been adopted. One set gives tentative standard temperatures and the other two list values of the probable minimum and the probable maximum temperatures for the entire world. These three sets of temperatures which were originally recommended by the Subcommittee on the Upper Atmosphere are given by linear variations with altitude between the points specified in the following tabulation of temperatures.

TEMPERATURES

Altitude (km)	Probable minimum (°K) (a)	Tentative standard (°K)	Probable maximum (°K) (a)
0	225	b ₂₈₈	320
10.76923		b ₂₁₈	
11			250
17	180		
20		b ₂₁₈	
25			255
32		218	
45	200		380
50		350	
55	300		
60		350	
70			380
78		240	
80	170		300
83		240	
120	300	375	600

^aThe values of ambient air temperature listed in these two columns are not intended to represent extreme values for the entire world, and for all time, but rather values that bracket the temperatures over nearly all the earth most all the time.

^bThese values are standard, and have been used previously in references 1, 3, 4, and 5.

These temperature-altitude relationships are also shown in figure 1.

Tentative Composition

The tentative composition used in computing the tables was arrived at by taking into consideration the fact that, at altitudes below 80 kilometers in the day time and below 105 kilometers at night, the generally accepted variations in chemical composition are too small to affect appreciably the computed pressures and densities. However, it is believed that at levels above those just specified significant changes in composition result from the dissociation of oxygen molecules by solar radiation. It is furthermore known that the presence of water vapor in the atmosphere does not appreciably affect pressures and densities. As a result of such considerations, and in the interest of simplicity, the following tentative specifications for composition of the upper atmosphere were recommended by the Subcommittee and have been adopted for the purposes of computing the values in these tables:

(1) For day time, the dissociation of oxygen is such as to produce a linear volume gradient from all-molecular oxygen at 80 kilometers to all-atomic oxygen at 100 kilometers. Except for oxygen dissociation, the composition is the same as that at sea level.

(2) For night time, the dissociation of oxygen is such as to produce a linear volume gradient from all-molecular oxygen at 105 kilometers to all-atomic oxygen at 120 kilometers. Except for oxygen dissociation the composition is the same as that at sea level.

(3) At altitudes below the regions of oxygen dissociation the composition is the same as that at sea level.

(4) At altitudes above the regions in which both molecular and atomic oxygen exist, as stipulated in (1) and (2), and up to at least 120 kilometers, the composition is the same as that at sea level, except for oxygen which is in the atomic rather than in the molecular form.

The variation with altitude of the specified molecular oxygen content of the atmospheres is graphically portrayed in figure 2.

PHYSICAL RELATIONSHIPS

Basic Equations

In addition to the specifications for temperature and composition already listed, certain other assumptions are made and

serve as the basis for deriving the various equations used in computing the properties of the upper atmosphere. These additional assumptions are:

- (a) The air is dry
- (b) The air behaves as a perfect gas and hence obeys the general gas law which may be written

$$\frac{P}{P_0} = \frac{P}{P_0} \frac{T_0}{T} \frac{M}{M_0} \quad (1)$$

- (c) The air is at rest with respect to the earth and hence obeys the basic law for fluid statics

$$dp = -g_0 dh \quad (2)$$

By means of equations (1) and (2) and equations representing the adopted specifications for temperature and composition, relationships may be deduced between pressure and height. The equations representing the adopted specifications are

$$T = T_1 + L(h - h_1) \quad (3)$$

where L is the temperature gradient $\Delta T/\Delta h$, and

$$\frac{M}{M_0} = \frac{1}{1 - K(h - h_m)} \quad (4)$$

where K is the volume gradient of oxygen dissociation $\Delta v/\Delta h$. The derivation of equation (4) is given in appendix A.

In addition to the three assumptions just listed, it is necessary to make an assumption concerning the value of the acceleration of gravity. For the purpose of furnishing tables for the upper atmosphere that will be consistent with the present standard tables for the lower atmosphere (reference 1), it is necessary to make the same assumption concerning the acceleration of gravity as was used in preparing the standard tables. This assumption is

- (d) For the tables based on a constant value of g the acceleration of gravity at all altitudes is the standard sea-level value; that is,

$$g = g_0 \quad (5)$$

For those instances in which closer conformity to actual conditions is required than is inherent in these tables it is necessary to make another assumption concerning the value of the acceleration of gravity. This assumption is

- (e) For tables based on a variable value of g the acceleration of gravity varies inversely as the square of the distance from the center of the earth; that is,

$$g = g_0 \left(\frac{r}{r + h} \right)^2 \quad (6)$$

Pressure-Height Relationships

By use of the foregoing basic equations and assumptions, other equations are derived which relate pressure to altitude. Two sets of equations are used, one set based on a constant value of g as specified in assumption (d), the other set based on the variation of g that is specified in assumption (e). The deductions for the first set are indicated in appendix B and for the second set in appendix C. The equations that are based on a constant value of g are as follows:

For combination A (constant temperature and constant composition):

$$\log_e \left(\frac{p}{p_A} \right) = C_A (h - h_A) \quad (7)$$

where

$$C_A = - \frac{g_0 \rho_0 T_0}{p_0} \frac{M}{T} \frac{M_0}{M} \quad (8)$$

For combination B (constant temperature gradient and constant composition):

$$\log \left(\frac{p}{p_B} \right) = C_B \log \left(\frac{T}{T_B} \right) \quad (9)$$

where

$$C_B = - \frac{g_0 \rho_0 T_0}{p_0 L} \frac{M}{M_0} \quad (10)$$

For combination C (constant temperature and constant volume gradient of dissociation) :

$$\log \left(\frac{p}{p_C} \right) = C_C \log \left(\frac{M}{M_C} \right) \quad (11)$$

where

$$C_C = - \frac{g_0 \rho_0 T_0}{p_0 K T} \quad (12)$$

For combination D (constant temperature gradient and constant volume gradient of dissociation) :

$$\log \left(\frac{p}{p_D} \right) = C_D \log \left(\frac{T}{T_D} \frac{M}{M_D} \right) \quad (13)$$

where

$$C_D = \frac{-g_0 \rho_0 T_0 M_D}{p_0 (M_0 + M_D T_D K)} \quad (14)$$

The equations derived in appendix C, based on a variable value of g , are more complex than those listed in the foregoing and consequently they are not reproduced here.

Speed of Sound

The speed of sound at any altitude relative to that at sea level is computed by the equation

$$\frac{a}{a_0} = \left(\frac{\gamma T M_0}{\gamma_0 T_0 M} \right)^{1/2} \quad (15)$$

where the ratio of the specific heats γ , as derived in appendix A, is

$$\frac{\gamma}{\gamma_0} = 1 - \frac{128K(h - h_m)}{21M_0} \quad (16)$$

The variation with altitude of the ratio of specific heats γ for the specified atmosphere is shown in figure 3(a).

Coefficient of Viscosity

Sutherland's equation for the variation of the coefficient of viscosity with temperature is used. It is

$$\frac{\mu}{\mu_0} = \left(\frac{T}{T_0}\right)^{3/2} \left(\frac{T_0 + S}{T + S}\right) \quad (17)$$

in which, according to reference 16,

$$S = 120$$

when the T's are in °K, and

$$S = 216$$

when the T's are in °F absolute.

A caution concerning the use of values obtained from equation (17) for the upper atmosphere is given in the section entitled "Discussion of Tables."

Molecular Mean Free Path

The ratio of the molecular mean free path at any altitude to the corresponding value at sea level is computed by

$$\frac{\lambda}{\lambda_0} = \frac{p_0 T_0}{p T_0 g_0} \quad (18)$$

This equation is justified in appendix D.

BASIC CONSTANTS

In the preceding section equations are given by means of which several properties of the upper atmosphere are computed. These computations involve numerical values of the several properties at sea level. Appendix E discusses the chosen sea-level values for

each of several properties of the atmosphere and they are listed in table I in both metric and British engineering systems of units. Values are listed for each of the three specified atmospheres and in some instances the quantity is expressed in more than one unit in either the metric or British system.

The values listed in table I for the standard atmosphere at sea level are identical with those used in references 1 and 5 except in a few instances. The exceptions are noted and explained in appendix E.

DISCUSSION OF TABLES

The appropriate equation (equation (7), (9), (11) or (13) for the constant value of g , or (C3), (C6), (C10) or (C13) for the variable values of g) is used to compute the ratio of the pressure p at any height to the pressure at the base of the region to which that particular equation applies. These pressure ratios for each of the regions are then used to compute the ratio of the pressure p to the pressure p_0 at sea level. These ratios p/p_0 are given in tables II to V.

By use of the computed values of the pressure ratios p/p_0 and of the sea-level value of pressure p_0 as given in table I, the value of the pressure p is computed and then given in tables II to V. The pressures given in tables IV and V are also plotted against altitude in figure 3(b).

The remaining quantities given in tables II to V are similarly computed by means of the appropriate equation and the corresponding sea-level value given in table I. The values for these remaining quantities given in tables IV and V are also shown plotted against altitude in figures 3(c) to 3(h).

Attention is directed to the fact that all tables in this report are based on the engineering system (sometimes referred to as the gravitational system) in which the fundamental quantities are length, force, and time. The standard units for force used herein are, therefore, pounds for the British system and kilograms for the metric system.

Accuracy of Computed Tables II to V

In tables II to V all quantities except the mean free paths of the molecules are tabulated to four significant figures, and the mean free paths of the molecules are tabulated to three significant figures. All computations for table II were carried through to six significant figures and consequently the values given in this table are believed to be exact.

Most of the values for table IV were obtained from table II by use of suitable conversion factors evaluated by a graphical method described in appendix C. The errors resulting from the method, and therefore the errors in the values tabulated in table IV are believed not to exceed 0.01 of 1 percent.

A method of graphical interpolation was applied to obtain from tables II and IV the values for use at the intermediate levels tabulated in tables III and V. The accuracy of this method is such as to introduce an error of not over one-twentieth of 1 percent in the values listed in tables III and V. Consequently, whenever a discrepancy exists between the metric and British values, the metric values should govern.

Validity of Tabulated Values at the Higher Altitudes

Pressure, density, specific weight, and mean free path of molecules. - As was previously mentioned, the computations for tables II and III are based on a constant value for the acceleration of gravity g so that the values listed would be consistent with those appearing in the present standard tables for the lower levels of the atmosphere (reference 1). The errors in the computed values of pressure, density, specific weight and mean free path inherent in the assumption of a constant value for the acceleration of gravity become progressively greater with increasing altitude, being about 30 percent at 120 kilometers. However, a variation of 30 percent in pressure at 120 kilometers corresponds to a variation of less than 4 percent in altitude at this level, and at lower levels the change in altitude corresponding to the error in pressure rapidly approaches zero. It is apparent therefore that in at least some applications the values in tables II and III will be adequate and therefore useful. Furthermore, they represent an extension of the present standard tables (reference 1).

In order to satisfy the need that may exist for values that are not affected by the use of a constant value for the acceleration of gravity g , tables IV and V are presented. In these tables g is assumed to vary inversely as the square of the

distance from the center of the earth. This assumption therefore takes into consideration the variation due to gravitational attraction, but it does not allow for the effect of centrifugal force. The centrifugal force due to the rotation of the earth is known to be only a small fraction of 1 percent of the gravitational force at an altitude of 120 kilometers, and consequently this omission does not result in a significant error.

The standard value used for the acceleration of gravity at sea level (and at all altitudes for tables II and III) is 9.80665 meters per second per second. This value corresponds rather closely to the true acceleration of gravity at sea level at latitude 45°. (More specifically, it corresponds to the theoretical acceleration of gravity at sea level and at latitude 45° 24' according to the International formula. See reference 17.) If still greater accuracy than is inherent in tables IV and V is required at latitudes far displaced from latitude 45°, an estimate of the latitude effect upon pressure and density may be obtained by use of the equation

$$\log \frac{p_\phi}{p_0} = \frac{g_{0\phi}}{g_0} \log \frac{p}{p_0} \quad (19)$$

where p_ϕ is the pressure at altitude h and at latitude ϕ , and $g_{0\phi}$ is the acceleration of gravity at sea level and at latitude ϕ . A similar equation (replacing p 's with ρ 's) applies to densities.

By means of equation (19) it can be shown that a latitude correction factor (L.C.F.) defined by

$$\text{L.C.F.} = \frac{p_\phi}{p} \quad (20)$$

can be computed by

$$\text{L.C.F.} = \left(\frac{p}{p_0} \right)^{\frac{g_{0\phi} - g_0}{g_0}} \quad (21)$$

If values of $g_{0\phi}$ from reference 17 are used, the following values for the exponent $(g_{0\phi} - g_0)/g_0$ are obtained:

Latitude (deg)	$\frac{g_{0\phi} - g_0}{g_0}$	Latitude (deg)	$\frac{g_{0\phi} - g_0}{g_0}$
0	-2.66758×10^{-3}	50	0.42175×10^{-3}
10	-2.50922	60	1.28372
20	-2.05299	70	1.98732
30	-1.35337	80	2.44701
40	-0.49405	90	2.60670

The foregoing exponents when applied to the values of pressure ratio p/p_0 tabulated in tables IV and V give the values of the latitude correction factor described by equations (20) and (21). For latitudes at increments of 10° and for altitudes at increments of 10 kilometers the latitude correction factors that are applicable to the pressures given in tables IV and V have been computed and are presented in table VI. By means of table VI it is therefore possible to obtain computed values of pressure which take into consideration the variation with latitude of the sea-level value of the acceleration of gravity g_0 . This computation may be made by use of equation (20) which may be written $p_\phi = (L.C.F.)p$.

Coefficient of viscosity and kinematic viscosity. - The Sutherland formula (equation (17)) is strictly applicable only to a gas of constant composition and to pressures which are not too small, and consequently the tabulated values for the coefficient of viscosity and for the kinematic viscosity are obviously not entirely reliable at the higher altitudes. However, the lack of data on the viscosity of oxygen in the atomic form does not permit at this time an estimation of the correction that is needed to allow for the specified dissociation. Furthermore, because of the fact that the effective value of the viscosity of a gas at very low pressure flowing over a body depends on the size and shape of the body, it is not practical to give a correction that will be applicable to more than one specific size and shape of a body. The values for viscosity at the higher altitudes should therefore be used with caution.

Speed of sound. - The tabulated values for the speed of sound are believed to be correct for all altitudes covered by the tables.

Caution should be exercised, however, in using the tabulated values for the upper altitudes in connection with Mach numbers because at high altitudes where the mean free paths of the air molecules are large in comparison with the dimensions of the body moving through them, the laws of fluid dynamics do not apply and the laws of particle dynamics must be used. When aerodynamic forces, for example, are computed for these conditions by use of the laws of particle dynamics the most probable speed of the air molecules is found to be the basic quantity rather than the speed of sound.

As in the case of viscosity, the altitude range in which the most probable speed of the air molecules replaces the speed of sound as the basic quantity depends upon the size of the body under consideration. It is consequently not possible to specify a single level at which the molecular speed becomes significant in aerodynamics. For this reason values for the speed of sound are listed to 120 kilometers.

In any case in which the most probable speed of the air molecules c is needed rather than the velocity of sound a it is possible to obtain the value of c from the value of a listed in the tables by use of the appropriate factor obtained from the following tabulation:

Altitude, h		Ratio of the most probable molecular speed to the speed of sound, $\frac{c}{a} = \sqrt{\frac{2}{\gamma}}$	
(m)	(ft)	Day	Night
80,000	262,467	1.195	1.195
85,000	278,871	1.189	1.195
90,000	295,275	1.183	1.195
95,000	311,679	1.176	1.195
100,000	328,083	1.170	1.195
105,000	344,487	1.170	1.195
110,000	360,892	1.170	1.187
115,000	377,296	1.170	1.179
120,000	393,700	1.170	1.170

CONCLUDING REMARKS

The fact should be emphasized that the values given in the tables for the upper atmosphere are only tentative and as such may become obsolete after a sufficient number of reliable direct

measurements of certain quantities have been made available. In the meantime these tentative tables should be useful not only in serving as a basis for comparing performance characteristics and estimating limiting values of performance, but also in securing the additional data needed for revising these tentative tables for the upper atmosphere.

Langley Memorial Aeronautical Laboratory
National Advisory Committee for Aeronautics
Langley Field, Va., December 6, 1946

APPENDIX A

VARIATION WITH ALTITUDE OF MOLECULAR WEIGHT

AND RATIO OF SPECIFIC HEATS

Molecular Weight in the Region of Oxygen Dissociation

Consider an initial unit volume of normal air composed only of molecular gases, consisting of oxygen and other constituents. Let all the non-oxygen constituents be diatomic of average molecular weight M_N , and let the molecular weight of oxygen in the molecular form be M_m , and in the atomic form M_a . Then

$$M_a = \frac{1}{2} M_m \quad (A1)$$

Let the initial conditions be as follows:

v_0 volume of all-molecular oxygen at height h_m

$1 - v_0$ volume of non-oxygen components at height h_m

M_0 average molecular weight of the initial air mixture at height h_m

Then

$$M_0 = v_0 M_m + (1 - v_0) M_N \quad (A2)$$

At height h , between h_m and h_a (where h_m is height at base of region in which dissociation occurs, and h_a is height at top of the region, and where all the oxygen is in the atomic form) the volume of molecular oxygen v_m per unit initial volume of normal air is

$$v_m = v_0 \left(\frac{h_a - h}{h_a - h_m} \right) \quad (A3)$$

and the volume of atomic oxygen v_a per unit initial volume of normal air is

$$v_a = 2v_0 \left(\frac{h - h_m}{h_a - h_m} \right) \quad (A4)$$

Therefore, the average molecular weight M of the atmosphere at height h can be shown to be

$$M = \frac{M_0}{1 - K(h - h_m)} \quad (A5)$$

where

$$K = -\frac{v_0}{h_a - h_m} \quad (A6)$$

the volume gradient of molecular oxygen, $\Delta v/\Delta h$.

Ratio of Specific Heats in the Region of Oxygen Dissociation

The ratio of specific heats γ for diatomic gases is taken to be $7/5$ and for monatomic gases, $5/3$. If the ratio of the specific heats γ for the atmosphere is assumed to be given by a weighted average, according to relative masses, of the values of γ for diatomic and monatomic gases, it can be shown, by using equations (A1), (A2), (A3), and (A4) that for those regions of the atmosphere in which dissociation of oxygen occurs

$$\gamma = \frac{7}{5} + \frac{4}{15} v_0 \left(\frac{M_m}{M_0} \right) \left(\frac{h - h_m}{h_a - h_m} \right) \quad (A7)$$

The standard value for v_0 , for the atmosphere at sea level, is $7/5$, and for M_m the standard value is 32. Therefore

$$\frac{\gamma}{v_0} = 1 - \frac{128K(h - h_m)}{21M_0} \quad (A8)$$

It is estimated that in the tentative standard atmosphere the variation of γ due to pressure and temperature effects is only about 0.6 of 1 percent. For this reason the effect of pressure and temperature upon γ is ignored in computing these tentative tables.

APPENDIX B

VARIATION OF PRESSURE WITH ALTITUDE (ASSUMING THE
ACCELERATION OF GRAVITY IS A CONSTANT g_0)

The equations relating atmospheric pressure to height for all altitude ranges in all three atmospheres (minimum, standard, and maximum temperatures) are only four in number. These four equations represent all possible combinations of the two types of temperature-height relationship and the two types of composition-height relationship. The deductions of the equations are based upon the familiar hydrostatic relation

$$dp = - g_0 \rho dh \quad (B1)$$

and upon the general gas equation

$$\frac{\rho}{\rho_0} = \frac{p}{p_0} \frac{M}{M_0} \frac{T_0}{T} \quad (B2)$$

These two equations, when combined, give

$$\frac{dp}{p} = - \frac{g_0 \rho_0 T_0 M}{p_0 T M_0} dh \quad (B3)$$

The differential equation (B3) is then used for deriving algebraic equations for pressure as a function of altitude, for each of the four combinations of temperature-height and composition-height relationships previously discussed. The derivations are indicated in the following paragraphs and the resulting equations are used in the preparation of tables II and III.

Combination A (constant temperature and constant composition). The type of atmosphere in which both the temperature and composition are constant may be represented algebraically by

$$T = \text{Constant}$$

and

$$M = \text{Constant}$$

Equation (B3) when integrated between the limits of height h_A and height h then becomes,

$$\log_e \left(\frac{p}{p_A} \right) = - \frac{g_0 \rho_0 T_0 M}{p_0 T M_0} (h - h_A) \quad (B4)$$

where h_A is the base of the region in which type A conditions prevail.

Combination B (constant temperature gradient and constant composition). - For the type of atmosphere having a constant temperature gradient and constant composition, let the temperature gradient be represented by

$$L = \text{Constant} = \frac{\Delta T}{\Delta h} \quad (B5)$$

and the temperature by

$$T = T_B + L(h - h_B) \quad (B6)$$

where T_B and h_B are the respective values at the base of the region to which combination B conditions prevail. Also $M = \text{Constant}$. Equation (B3) then becomes

$$\frac{dp}{p} = \left(- \frac{g_0 \rho_0 T_0 M}{p_0 M_0} \right) \frac{dh}{T_B + L(h - h_B)} \quad (B7)$$

and when integrated between the limits of h_B and h this equation becomes

$$\log \left(\frac{p}{p_B} \right) = - \frac{g_0 \rho_0 T_0 M}{p_0 M_0} \log \left(\frac{T}{T_B} \right) \quad (B8)$$

Combination C (constant temperature and constant volume gradient of dissociation). - In the type of atmosphere where both the temperature and volume gradient of dissociation are constant

$$T = \text{Constant}$$

and an expression for M as a function of h is derived in appendix A, and it is found to be

$$M = \frac{M_0}{1 - K(h - h_m)} \quad (B9)$$

where K is the volume gradient of molecular oxygen defined by

$$K = \frac{\Delta v}{\Delta h} = \text{Constant} \quad (B10)$$

Using these relationships with equation (B3) gives

$$\frac{dp}{p} = - \frac{s_0 p_0 T_0 dh}{p_0 T [1 - K(h - h_m)]} \quad (B11)$$

Integrating equation (B11) between the limits of h_C and h , where h_C is the height at the base of the region in which type C conditions prevail, gives

$$\log \left(\frac{p}{p_C} \right) = \frac{s_0 p_0 T_0}{p_0 T K} \log \left(\frac{M_C}{M} \right) \quad (B12)$$

Combination D (constant temperature gradient and constant volume gradient of dissociation). - The type of atmosphere having both the temperature gradient and the volume gradient of dissociation constant is referred to as combination D. For this combination, the expression for molecular weight given in equation (B9) and an appropriate modification of equation (B6) give, for equation (B3), the following equation:

$$\frac{dp}{p} = - \frac{s_0 p_0 T_0 dh}{p_0 [1 - K(h - h_m)] [T_D + L(h - h_D)]} \quad (B13)$$

Integrating the variable part of the right-hand member, between the limits of h_D and h , gives

$$\frac{1}{(1 + Kh_m)L + (T_D - Lh_D)K} \log \left[\frac{T_D + L(h - h_D)}{1 - K(h - h_m)} \right] \Big|_{h_D}^h$$

Therefore

$$\log \left(\frac{p}{p_D} \right) = \frac{-g_0 \rho_0 T_0 M_D}{p_0 (M_0 L + M_D K T_D)} \log \left(\frac{T_M}{T_D M_D} \right) \quad (B14)$$

APPENDIX C

VARIATION OF PRESSURE WITH ALTITUDE (ASSUMING THE ACCELERATION
 OF GRAVITY VARIES INVERSELY AS THE SQUARE OF THE
 DISTANCE FROM THE CENTER OF THE EARTH)

The equations relating pressure and altitude derived herein are based upon the general differential equation derived from equation (B2) of appendix B, from the hydrostatic relation

$$\frac{dp}{p} = -g_0 dh \quad (C1)$$

and from the equation representing the inverse square variation of the acceleration of gravity

$$g = g_0 \left(\frac{r}{r + h} \right)^2 \quad (C2)$$

This general differential equation is

$$\frac{dp}{p} = \frac{-g_0 p_0 T_0 M r^2 dh}{p_0 T_0 M_0 (r + h)^2} \quad (C3)$$

As in appendix B four equations are deduced for use in each of the four possible combinations of specified temperature-altitude and composition-altitude relationships. The resulting algebraic equations are used in the preparation of tables IV and V. The deductions for each combination are indicated in the following paragraphs.

Combination A (constant temperature and constant composition). For combination A (constant temperature and constant pressure) the algebraic equation relating pressure and altitude is obtained by integrating equation (C3) between the limits of altitude h_A and h . The result is

$$\log_e \left(\frac{p}{p_A} \right)_g = \frac{-g_0 p_0 T_0 M}{p_0 T_0 M_0} \frac{r^2 (h - h_A)}{(r + h)(r + h_A)} \quad (C4)$$

(Note that in this equation and succeeding equations the subscript g is used to indicate values computed with the variation in the acceleration of gravity that is specified by equation (C2).)

Combination B (constant temperature gradient and constant composition). - For combination B (constant temperature gradient and constant composition) the differential equation is obtained by substituting in equation (C3) the value for T given by

$$T = T_B + L(h - h_B) \quad (C5)$$

The differential equation is then

$$\frac{dp}{p} = \frac{-g_0 p_0 T_0 M r^2 dh}{p_0 M_0 [T_B + L(h - h_B)] (r + h)^2} \quad (C6)$$

The algebraic equation obtained by integrating equation (C6) between the appropriate limits is

$$\log_e \left(\frac{p}{p_B} \right)_g = C_{B_g} \left[\frac{r(h - h_B)}{(r + h)(r + h_B)} + \frac{rL}{rL + h_B L - T_B} \log_e \frac{(r + h)T_B}{(r + h_B)T} \right] \quad (C7)$$

where

$$C_{B_g} = \frac{g_0 p_0 T_0 M}{p_0 M_0 \left[L - \frac{1}{r}(T_B - Lh_B) \right]} \quad (C8)$$

Combination C (constant temperature and constant volume gradient of dissociation). - For combination C (constant temperature and constant volume gradient of dissociation) the differential equation is obtained by substituting in equation (C3) the value of M given by

$$M = \frac{M_0}{1 - K(h - h_m)} \quad (C9)$$

The differential equation is then

$$\frac{dp}{p} = \frac{-g_0 p_0 T_0 r^2 dh}{p_0 T [1 - K(h - h_m)] (r + h)^2} \quad (C10)$$

The algebraic equation obtained by integrating equation (C10) between appropriate limits is

$$\log_e \left(\frac{p}{p_C} \right)_g = C_{Cg} \left\{ \left[\frac{\frac{K}{1 + Kh_C}}{K + \frac{1 + Kh_C}{r}} \log_e \frac{M(r + h)}{M_0(r + h_C)} \right] - \frac{r(h_C - h)}{(r + h)(r + h_C)} \right\} \quad (C11)$$

where

$$C_{Cg} = \frac{-g_0 p_0 T_0}{p_0 T \left(K + \frac{1 + Kh_C}{r} \right)} \quad (C12)$$

Combination D (constant temperature gradient and constant volume gradient of dissociation). - For combination D (constant temperature gradient and constant volume gradient of dissociation) the differential equation is obtained by substituting in equation (C3) the values of T and M given by a slightly modified form of equation (C5) and by equation (C9), respectively. The resulting differential equation is then

$$\frac{dp}{p} = \frac{-g_0 p_0 T_0 r^2 dh}{p_0 [T_D + L(h - h_D)] [1 - K(h - h_m)] (r + h)^2} \quad (C13)$$

The algebraic equation obtained by integrating equation (C13) between appropriate limits is

$$\begin{aligned} \log_e \left(\frac{p}{p_D} \right)_g &= C_{Dg} \left[\frac{a(h - h_D)}{(1 + xh)(1 + xh_D)} + \frac{b}{x} \log_e \left(\frac{1 + xh}{1 + xh_D} \right) \right. \\ &\quad \left. + \frac{c}{y} \log_e \left(\frac{1 + yh}{1 + yh_D} \right) + \frac{d}{z} \log_e \left(\frac{1 + zh}{1 + zh_D} \right) \right] \end{aligned} \quad (C14)$$

where

$$C_{D3} = \frac{-g_0 p_0 T_0}{p_0 (T_D - L h_D) (1 + kh_m)} \quad (C15)$$

$$x = \frac{1}{r}$$

$$y = \frac{L}{(T_D - L h_D)}$$

$$z = \frac{-K}{(1 + kh_m)}$$

$$a = \frac{x^2(x^2 + yz - yx - zx)}{(z - x)^2(y - x)^2}$$

$$\frac{b}{x} = \frac{x(2yz - xy - xz)}{(z - x)^2(y - x)^2}$$

$$\frac{c}{y} = \frac{-y^2}{(y - x)^2(z - y)}$$

$$\frac{d}{z} = \frac{z^2}{(z - x)^2(z - y)}$$

Equations (C4), (C7), (C11), and (C14) were used to compute the pressure ratios at the transition levels only in the tentative standard atmosphere. By dividing these pressure ratios by the pressure ratios at the same transition levels obtained by use of the equations in appendix B based on a constant value for the acceleration of gravity, a conversion factor was obtained for each of the several transition altitudes. Since it was impractical to use these complex equations for directly computing the pressure

ratios at all the levels recorded in tables IV and V, the values at these numerous intermediate levels were arrived at as follows:

(1) For each altitude a value for the conversion factor was computed by algebraic summation from the equation

$$\log_e \left(\frac{p_g}{p} \right) = \frac{p_0 T_0}{p_0 M_0} \sum_0^h (g_0 - g) \frac{M}{T} \Delta h \quad (C16)$$

where p_g is the pressure based on the variable value of g , and p is the pressure based on a constant value for the acceleration of gravity. In equation (C16) the proper value of g , T , and of M was substituted for each region of the atmosphere, according to equation (C2), (C5), and (C9), respectively.

(2) The values of p_g/p so computed were plotted against altitude to define the shape of the curve relating pressure ratios to altitude.

(3) The accurate values for the pressure ratio computed by equations (C4), (C7), (C11), and (C14) and by equations (B4), (B8), (B12), and (B14) were also plotted and another curve was drawn through these points representing the accurately computed ratios and faired according to the curve drawn through the points obtained by use of equation (C16).

(4) The curve arrived at from step (3) was then used to obtain conversion factors for each of the altitudes recorded in tables IV and V.

APPENDIX D

MOLECULAR MEAN FREE PATHS

Ratio of the Mean Free Paths of Molecules

The conventional equation for the mean free path of the molecules λ of a gas (reference 18) is

$$\lambda = \frac{1}{\pi \sqrt{2} N \sigma^2} \quad (D1)$$

Therefore the ratio of the mean free path at any altitude to the value at sea level is

$$\frac{\lambda}{\lambda_0} = \frac{N_0}{N} \left(\frac{\sigma_0}{\sigma} \right)^2 \quad (D2)$$

But

$$N_m = \rho \quad (D3)$$

and

$$\sigma_0 = \frac{pM}{kT} \quad (D4)$$

Therefore

$$\frac{N_0}{N} = \frac{p_0}{p} \frac{T}{T_0} \frac{g}{g_0} \quad (D5)$$

and

$$\frac{\lambda}{\lambda_0} = \frac{p_0}{p} \frac{T}{T_0} \frac{g}{g_0} \left(\frac{\sigma_0}{\sigma} \right)^2 \quad (D6)$$

For all constituents of the atmosphere except oxygen in the region of dissociation,

$$\sigma = \sigma_0$$

In the absence of available data on the diameter of atoms of oxygen relative to that of molecular oxygen, and in consideration of the fact that the small difference in these two diameters of oxygen has an even smaller effect upon the average diameter of all atmospheric constituents, and for reasons of simplicity it is herein assumed for oxygen also that $\sigma = \sigma_0$. For the purpose of computing these tables therefore equation (D6) is simplified to

$$\frac{\lambda}{\lambda_0} = \frac{P_0 \cdot T}{P \cdot T_0} \frac{g}{g_0} \quad (D7)$$

Furthermore, in those computations that are based on a constant value for the acceleration of gravity

$$g = g_0$$

whence equation (D7) is further simplified to

$$\frac{\lambda}{\lambda_0} = \frac{P_0}{P} \frac{T}{T_0} \quad (D8)$$

Mean Free Paths of Molecules at Sea Level

The values of the mean free path of the molecules at sea level given in table I are for nitrogen and oxygen molecules in a normal atmospheric mixture of nitrogen and oxygen. These mean free paths are designated λ_n and λ_o , respectively. A weighted average of the foregoing mean free paths, based upon the relative volumes of nitrogen and oxygen in air is also included and is designated λ_{air} .

The mean free path of the nitrogen molecules in the atmosphere at sea level was computed by the following formula (p. 99 of reference 18):

$$\lambda_n = \frac{1}{\pi \sqrt{2} N_n \sigma_n^2 + \pi N_o \sigma_o^2 \frac{\sqrt{\bar{c}_n^2 + \bar{c}_o^2}}{\bar{c}_n}}$$

where

- N_n number of nitrogen molecules per unit volume of air
- N_o number of oxygen molecules per unit volume of air
- σ_n diameter of nitrogen molecules
- σ_o diameter of oxygen molecules
- $\bar{\sigma}$ average diameter of nitrogen and oxygen molecules
- \bar{c}_n average speed of nitrogen molecules
- \bar{c}_o average speed of oxygen molecules

Similarly, the mean free path of the oxygen molecules at sea level was computed by

$$\lambda_o = \frac{1}{\pi \sqrt{2} N_o \sigma_o^2 + \pi N_n \bar{\sigma}^2 \frac{\bar{c}_n^2 + \bar{c}_o^2}{\bar{c}_o}} \quad (D9)$$

The values for the average speeds \bar{c}_n and \bar{c}_o were obtained from the formula $\bar{c} = \sqrt{\frac{3RT}{M}}$. The values for σ were taken from appendix III, column 4, of reference 18. Values of N_n and N_o , the number of molecules of nitrogen and oxygen, respectively, per unit volume were calculated from the Loschmidt number and the relative volume of the nitrogen and oxygen in air at sea level.

APPENDIX E

VALUES OF CERTAIN CONSTANTS

Tentative Standard Atmosphere at Sea Level

The standard sea-level values for various properties of the atmosphere have been listed in reference 1, and sea-level values for certain other properties are listed in reference 5. Most of these previously listed values are adopted for use in computing the tables herein, but a few changes have been made. The changes are as follows:

Speed of sound.- The values for the speed of sound have been altered slightly to avoid the discrepancy which existed between the values previously listed and the values computed by the conventional equation

$$a_0 = \sqrt{\frac{\gamma_0 p_0}{\rho_0}} \quad (\text{E1})$$

The values for a_0 listed in table I are computed according to equation (E1) by using the appropriate values for γ_0 , p_0 , and ρ_0 that are also listed in table I.

Density.- The values for density in the British engineering system has been changed from 0.002378 to 0.0023779 slugs per cubic foot to avoid discrepancies resulting when computations are based either on the standardized value for specific weight, 1.2255 kilograms per cubic meter (reference 1), or on the derived value for density.

Molecular mean free paths and molecular weight.- In addition to the various quantities previously given in references 1 and 5, the present paper lists molecular mean free paths and the average molecular weight of normal sea-level air. Molecular mean free paths for the nitrogen molecules and oxygen molecules in the normal air mixture have been computed and a weighted average for air has been taken, as described in appendix D. The average molecular weight of normal sea-level air is taken as 28.966 in accordance with reference 19.

Pressure.-- The value for pressure in the British engineering system has been changed from 407.1 or 407.2 inches of water at 15° C as used in reference 5 and reference 26, respectively, to 407.15 inches of water at 15° C. This value of 407.15 is the computed value corresponding to 760 millimeters of mercury based on the auxiliary constants and conversion factors listed in the last section of this appendix E.

Table of Sea-Level Values

The values for the various properties of the atmosphere at sea level corresponding to the adopted values for probable minimum and probable maximum temperatures are computed from the values corresponding to standard sea-level temperatures. All three sets of values used in both metric and British engineering systems of units are tabulated in table I. In some instances a quantity is listed in more than one unit, in either the metric or British system.

Auxiliary Constants and Conversion Factors

In addition to the atmospheric properties at sea level given in table I certain other basic constants and conversion factors are used in computing tables II to V. They are

Auxiliary constants:

Density of mercury at 0° C, gm/cm ³	13.5951
Standard acceleration of gravity, g ₀ , cm/sec ²	980.665
Density of water at 15° C, gm/ml	0.9991286
Radius of the earth at 45° latitude and at sea level, m	6,367,623

Conversion factors:

$$1 \text{ lb} = 453.5924 \text{ gm}$$

$$1 \text{ meter} = 3.280833 \text{ ft}$$

$$^{\circ}\text{K} = ^{\circ}\text{C} + 273$$

$$^{\circ}\text{F abs} = ^{\circ}\text{F} + 459.4$$

$$1 \text{ ml} = 1.000027 \text{ cm}^3$$

REFERENCES

1. Diehl, Walter S.: Standard Atmosphere - Tables and Data. NACA Rep. No. 218, 1925. (Reprint 1940.)
2. Gregg, Willis Ray: Standard Atmosphere. NACA Rep. No. 147, 1922.
3. Brombacher, W. G.: Tables for Calibrating Altimeters and Computing Altitudes Based on the Standard Atmosphere. NACA Rep. No. 246, 1926.
4. Brombacher, W. G.: Altitude-Pressure Tables Based on the United States Standard Atmosphere. NACA Rep. No. 538, 1935.
5. Aiken, William S., Jr.: Standard Nomenclature for Airspeeds with Tables and Charts for Use in Calculation of Airspeed. NACA TN No. 1120, 1946. **NACA Report No. 837**
6. Anon.: Meteorological Aspects of High-Altitude Flight. Rep. No. 847, Weather Div., Headquarters AAF, Dec. 1944. (Now distributed by Headquarters, Air Weather Service, Air Transport Command.)
7. Ratner, Benjamin: Temperature Frequencies in the Upper Air. Weather Bur., U. S. Dept. Commerce, Jan. 1946.
8. Martyn, D. F., and Pulley, O. O.: The Temperature and Constituents of the Upper Atmosphere. Proc. Roy. Soc. (London), ser. A, vol. 154, no. 882, April 1, 1936, pp. 455-486.
9. Pekeris, C. L.: Atmospheric Oscillations. Proc. Roy. Soc. (London), ser. A, vol. 158, no. 895, Feb. 3, 1937, pp. 650-671.
10. Martyn, D. F.: The Upper Atmosphere. C - General Discussion. Quarterly Jour. Roy. Meteorol. Soc., vol. 65, no. 281, 1939, pp. 328-330.
11. Penndorf, R.: Die Temperatur der hohen Atmosphäre. Meteorol. Zeitschr., Bd. 58, Heft 1, Jan. 1941, pp. 1-10. (Translation in Full. American Meteorol. Soc., vol. 27, no. 6, June 1946, pp. 331-342.)
12. Whipple, Fred L.: Meteors and the Earth's Upper Atmosphere. Rev. Modern Phys., vol. 15, no. 4, Oct. 1943, pp. 246-264.
13. Gutenberg, B.: Physical Properties of the Atmosphere Up to 100 Km. Jour. Meteorology, vol. 3, June 1946, pp. 27-30.

14. Wulf, Oliver R., and Deming, Lola S.: On the Production of the Ionospheric Regions E and F and the Lower-Altitude Ionization Causing Radio Fade-Outs. *Terr. Mag.*, vol. 43, no. 3, Sept. 1938, pp. 283-298.
15. Anon.: Nomenclature for Aeronautics. NACA Rep. No. 474, 1941.
16. Bircumshaw, L. L., and Stott, Vaughan H.: Viscosity of Gases. *International Critical Tables*, first ed., vol. V. McGraw-Hill Book Co., Inc., 1929, p. 1.
17. Anon.: Theoretical Gravity at Sea Level for Each Minute of Latitude by the International Formula. U. S. Dept. of Commerce, Coast and Geodetic Survey, 1942.
18. Loeb, Leonard B.: The Kinetic Theory of Gases. Second ed., McGraw-Hill Book Co., Inc., 1934.
19. Wildt, Rupert: The Geochemistry of the Atmosphere and the Constitution of the Terrestrial Planets. *Rev. Modern Phys.*, vol. 14, nos. 2-3, April-July 1942, p. 152.
20. Beij, K. Hilding: Aircraft Speed Instruments. NACA Rep. No. 420, 1932.

TABLE I.—PROPERTIES OF THE ATMOSPHERE AT SEA LEVEL

Quantity	Symbol	Metric engineering system				British engineering system			
		Unit	At probable minimum temperature	At standard temperature	At probable maximum temperature	Unit	At probable minimum temperature	At standard temperature	At probable maximum temperature
Temperature	t_0	$^{\circ}\text{C}$	-48.0	15.0	47.0	$^{\circ}\text{F}$	-54.5	59.0	116.6
Absolute temperature	T_0	$^{\circ}\text{K}$	225.0	288.0	320.0	$^{\circ}\text{F}$ abs.	405.0	518.4	576.0
Pressure	p_0	mm Hg at 0°C	760	760	760	in. Hg at 32°F	29.9212	29.9212	29.9212
		kg/m ²	10332.3	10332.3	10332.3	in. water at 15°C	407.15	407.15	407.15
Specific weight	w_0	dynes/cm ²	1.01325×10^6	1.01325×10^6	1.01325×10^6	lb/ft ²	2116.23	2116.23	2116.23
Density	$\rho_0 = \frac{w_0}{g_0}$	kg/m ³	1.5636	1.2255	1.1030	lb/ft ³	0.097928	0.076506	0.068855
Coefficient of viscosity	μ_0	dynes/cm ²	1.5383	1.2018	1.0816	slugs/ft ³	0.0030437	0.0023779	0.0021401
Kinematic viscosity	$v_0 = \frac{\mu_0}{\rho_0}$	kg-sec ² /m ⁴	0.15995	0.124966	0.11247	lb-sec/ft ²	3.0420×10^{-7}	3.7250×10^{-7}	4.0455×10^{-7}
Speed of sound	a_0	m/sec	1.4852×10^{-6}	1.8187×10^{-6}	1.9751×10^{-6}	ft ² /sec	0.99944×10^{-4}	1.5665×10^{-4}	1.8903×10^{-4}
		km/hr	300.72	340.22	358.63	ft/sec	986.61	1116.22	1176.60
Mean free path of nitrogen molecules	λ_n	m	5.76×10^{-8}	7.38×10^{-8}	8.20×10^{-8}	mph	672.69	761.06	802.23
Mean free path of oxygen molecules	λ_o	m	5.75×10^{-8}	7.36×10^{-8}	8.18×10^{-8}	knots	584.16	660.90	696.65
Mean free path of air molecules	λ_{air}	m	5.76×10^{-8}	7.37×10^{-8}	8.19×10^{-8}	ft	0.1891×10^{-6}	0.2421×10^{-6}	0.2690×10^{-6}
Average molecular weight	M_0	----	28.966	28.966	28.966	ft	0.1887×10^{-6}	0.2415×10^{-6}	0.2683×10^{-6}
Ratio of specific heats	γ_0	----	1.4	1.4	1.4	----	1.4	1.4	1.4
Relative volume of oxygen	r_0	----	0.2095	0.2095	0.2095	----	0.2095	0.2095	0.2095

TABLES II AND III

PROPERTIES OF THE UPPER ATMOSPHERE
FOR TENTATIVE STANDARD TEMPERATURES
BASED ON AN ARBITRARY CONSTANT VALUE
OF GRAVITATIONAL FORCE

The following set of two tables (tables II and III) constitutes a consistent extension of the standard tables for the lower atmosphere (NACA Rep. No. 218). Consequently, altitudes in this set of tables which correspond to specified ambient-air pressures may be referred to as "tentative pressure altitudes," and those which correspond to a specified ambient-air density may be referred to as "tentative density altitudes" (NACA Rep. No. 474).

NATIONAL ADVISORY
COMMITTEE FOR AERONAUTICS.

TABLE II.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY
CONSTANT VALUE OF GRAVITATIONAL FORCE — METRIC ENGINEERING SYSTEM

Altitude, h (m)	Absolute temperature, T (°K)	Pressure, P (kg/m ²)	Pressure ratio, P/P ₀	Density, ρ (kg-m ⁻³)	Density ratio, ρ/ρ ₀	Specific weight, γ (kg/m ³)	Coefficient of viscosity, μ (kg-sec) m ²	Kinematic viscosity, ν = μ P (m ² /sec)	Speed of sound, c (m/sec)	Mean free path of molecules, λ (m)
(a) For both day and night										
20,000	218.0	563.0	5110x10 ⁻⁵	8839x10 ⁻⁶	7198x10 ⁻⁵	8822x10 ⁻⁵	1.146x10 ⁻⁶	0.01607x10 ⁻²	295.0	0.00162x10 ⁻³
20,000	218.0	520.5	503.8	8918	6855	8157	1.146	0.01738	295.0	0.00111
21,000	218.0	487.0	4658	7590	6585	7246	1.146	0.01850	295.0	0.00120
22,000	218.0	454.5	4307	7110	5690	6743	1.146	0.02033	295.0	0.00130
23,000	218.0	421.0	3983	6775	5261	6448	1.146	0.02159	295.0	0.00140
23,000	218.0	388.5	3683	6080	4968	5962	1.146	0.02378	295.0	0.00151
23,000	218.0	351.0	3405	5622	4493	5513	1.146	0.02572	295.0	0.00164
23,000	218.0	322.5	3148	5195	4259	5097	1.146	0.02762	295.0	0.00177
24,000	218.0	290.0	2811	4865	3948	4713	1.146	0.03008	295.0	0.00192
24,000	218.0	270.1	2692	4447	3595	4353	1.146	0.03234	295.0	0.00207
25,000	218.0	257.0	2489	4109	3288	4030	1.146	0.03518	295.0	0.00224
25,000	218.0	240.0	2304	3600	2741	3745	1.146	0.03848	295.0	0.00244
26,000	218.0	226.0	203.3	2958	2611	3128	1.146	0.04112	295.0	0.00262
27,000	218.0	203.9	1988	2593	2328	2945	1.146	0.04451	295.0	0.00284
27,000	218.0	188.3	1819	2004	2405	2745	1.146	0.04813	295.0	0.00307
28,000	218.0	173.8	1682	2777	2222	2727	1.146	0.05206	295.0	0.00332
28,000	218.0	160.7	1555	2668	2053	2518	1.146	0.05630	295.0	0.00359
29,000	218.0	148.6	1438	2373	1900	2329	1.146	0.06089	295.0	0.00388
29,000	218.0	137.4	1330	2195	1757	2153	1.146	0.06525	295.0	0.00419
29,000	218.0	127.1	1230	2030	1625	1991	1.146	0.07122	295.0	0.00454
30,000	218.0	117.8	1137	1878	1503	1841	1.146	0.07700	295.0	0.00490
30,000	108.6	1051	1736	1589	1702	1446	0.08330	295.0	0.00532	
31,000	218.0	100.0	9262	1474	1174	1146	0.09359	295.0	0.00574	
32,000	218.0	94.87	8769	1384	1087	1146	0.10389	295.0	0.00612	
33,000	218.0	89.77	8261	1291	996	1243	0.1146	0.1048	295.0	0.00651
34,000	218.0	79.45	789.0	1249	999.1	1224	0.1267	0.1175	295.0	0.00718
34,000	218.0	73.61	712.4	1138	910.5	1116	0.1387	0.1307	300.4	0.00809
34,000	218.0	68.26	660.8	1039	819.0	1082	0.1508	0.1452	303.4	0.00887
34,000	218.0	63.43	613.7	946.3	759.6	930.9	0.1620	0.1510	306.8	0.00970
34,000	218.0	58.95	570.5	993.3	852.1	948.0	0.1742	0.1606	308.2	0.01056
35,000	210.0	54.87	531.1	796.4	637.3	781.0	0.1968	0.1969	310.6	0.01216
35,000	210.0	51.13	424.9	731.0	484.9	716.9	0.2172	0.2172	312.9	0.0126
35,000	210.0	47.69	461.6	675.7	527.4	696.1	0.2393	0.2393	315.3	0.0137
35,000	210.0	44.26	412.6	580.0	462.6	601.6	0.2604	0.2604	317.6	0.0150
35,000	210.0	40.83	362.9	526.4	455.6	558.3	0.2827	0.2827	319.9	0.0163
35,000	210.0	38.40	329.8	376.9	328.1	420.2	0.3055	0.3173	322.5	0.0175
35,000	210.0	36.17	303.0	348.9	388.0	475.5	0.3285	0.3476	326.8	0.0190
35,000	210.0	34.16	280.8	330.8	348.6	432.7	0.3503	0.3686	329.0	0.0206
35,000	210.0	32.07	258.0	310.8	348.3	406.5	0.3724	0.3934	331.2	0.0224
35,000	210.0	30.00	237.0	291.4	307.4	376.8	0.4535	0.4535	334.2	0.0240
35,000	210.0	28.00	223.0	273.9	306.3	342.4	0.7644	0.7644	333.5	0.0259
35,000	210.0	26.00	210.0	257.4	285.6	325.3	1.1268	1.1268	335.8	0.0278
35,000	210.0	24.00	197.0	238.4	265.7	301.1	1.579	1.579	338.1	0.0296
35,000	210.0	22.00	184.0	225.3	252.7	280.6	1.835	1.835	340.4	0.0316
35,000	210.0	20.00	171.0	211.1	231.1	256.6	1.872	1.872	342.7	0.0336
35,000	210.0	18.00	158.0	201.2	212.6	211.5	1.950	1.950	345.0	0.0356
35,000	210.0	16.00	145.0	188.0	181.2	197.5	2.061	2.061	347.3	0.0376
35,000	210.0	14.00	132.0	175.0	170.2	184.7	2.098	2.098	349.6	0.0396
35,000	210.0	12.00	119.0	162.0	161.0	172.8	2.115	2.115	351.9	0.0416
35,000	210.0	10.00	106.0	151.0	152.2	161.7	2.147	2.147	354.2	0.0436
35,000	210.0	8.00	93.0	141.0	141.0	172.8	2.193	2.193	356.5	0.0456
35,000	210.0	6.00	80.0	130.0	132.0	162.6	2.208	2.208	358.8	0.0476
35,000	210.0	4.00	67.0	120.0	125.0	142.1	2.206	2.206	361.0	0.0496
35,000	210.0	2.00	54.0	110.0	123.0	136.0	2.013	2.013	363.1	0.0516
35,000	210.0	0.00	41.0	100.0	102.0	102.0	2.030	2.030	365.1	0.0536
35,000	210.0	39.00	39.00	98.20	98.01	98.05	2.058	2.058	367.1	0.0556
35,000	210.0	37.00	37.00	96.03	96.31	117.7	2.047	2.047	369.1	0.0576
35,000	210.0	35.00	35.00	94.00	94.97	110.7	2.065	2.065	371.1	0.0596
35,000	210.0	33.00	33.00	92.00	92.01	104.1	2.081	2.081	373.1	0.0616
35,000	210.0	31.00	31.00	90.00	90.01	98.05	2.098	2.098	375.1	0.0636
35,000	210.0	29.00	29.00	88.00	88.01	96.04	2.115	2.115	377.1	0.0656
35,000	210.0	27.00	27.00	86.00	86.01	94.03	2.132	2.132	379.1	0.0676
35,000	210.0	25.00	25.00	84.00	84.01	92.02	2.149	2.149	381.1	0.0696
35,000	210.0	23.00	23.00	82.00	82.01	89.01	2.166	2.166	383.1	0.0716
35,000	210.0	21.00	21.00	80.00	80.01	86.01	2.183	2.183	385.1	0.0736
35,000	210.0	19.00	19.00	78.00	78.01	83.01	2.200	2.200	387.1	0.0756
35,000	210.0	17.00	17.00	76.00	76.01	79.01	2.217	2.217	389.1	0.0776
35,000	210.0	15.00	15.00	74.00	74.01	75.01	2.234	2.234	391.1	0.0796
35,000	210.0	13.00	13.00	72.00	72.01	72.01	2.251	2.251	393.1	0.0816
35,000	210.0	11.00	11.00	70.00	70.01	69.01	2.268	2.268	395.1	0.0836
35,000	210.0	9.00	9.00	68.00	68.01	68.01	2.285	2.285	397.1	0.0856
35,000	210.0	7.00	7.00	66.00	66.01	66.01	2.302	2.302	399.1	0.0876
35,000	210.0	5.00	5.00	64.00	64.01	64.01	2.319	2.319	401.1	0.0896
35,000	210.0	3.00	3.00	62.00	62.01	62.01	2.336	2.336	403.1	0.0916
35,000	210.0	1.00	1.00	60.00	60.01	60.01	2.353	2.353	405.1	0.0936
35,000	210.0	-1.00	-1.00	58.00	58.01	58.01	2.370	2.370	407.1	0.0956
35,000	210.0	-3.00	-3.00	56.00	56.01	56.01	2.387	2.387	409.1	0.0976
35,000	210.0	-5.00	-5.00	54.00	54.01	54.01	2.404	2.404	411.1	0.0996
35,000	210.0	-7.00	-7.00	52.00	52.01	52.01	2.421	2.421	413.1	0.1016
35,000	210.0	-9.00	-9.00	50.00	50.01	50.01	2.438	2.438	415.1	0.1036
35,000	210.0	-11.00	-11.00	48.00	48.01	48.01	2.455	2.455	417.1	0.1056
35,000	210.0	-13.00	-13.00	46.00	46.01	46.01	2.472	2.472	419.1	0.1076
35,000	210.0	-15.00	-15.00	44.00	44.01	44.01	2.489	2.489	421.1	0.1096
35,000	210.0	-17.00	-17.00	42.00	42.01	42.01	2.506	2.506	423.1	0.1116
35,000	210.0	-19.00	-19.00	40.00	40.01	40.01	2.523	2.523	425.1	0.1136
35,000	210.0	-21.00	-21.00	38.00	38.01	38.01	2.540	2.540	427.1	0.1156
35,000	210.0	-23.00	-23.00	36.00	36.01	36.01	2.557	2.557	429.1	0.1176
35,000	210.0	-25.00	-25.00	34.00	34.01	34.01	2.574	2.574	431.1	0.1196
35,000	210.0	-27.00	-27.00	32.00	32.01	32.01	2.591	2.591	433.1	0.1216
35,000	210.0	-29.00	-29.00	30.00	30.01	30.01	2.608	2.608	435.1	0.1236
35,000	210.0	-31.00	-31.00	28.00	28.01	28.01	2.625	2.625	437.1	0.1256
35,000	210.0	-33.00	-33.00	26.00	26.01	26.01	2.642	2.642	439.1	0.1276
35,000	210.0	-35.00	-35.00	24.00	24.01	24.01	2.659	2.659	441.1	0.1296

TABLE II.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY
CONSTANT VALUE OF GRAVITATIONAL FORCE—METRIC ENGINEERING SYSTEM—Concluded

Altitude, h (m)	Absolute tempera- ture, T (°K)	Pressure, P (kg/m ²)	Pressure ratio, P/P ₀	Density, ρ (kg-sec ²) m ⁻⁴	Density ratio, σ = ρ/ρ ₀	Specific weight, γ = ρg (kg/m ³)	Coefficient of viscosity, μ (kg-sec) m ²	Kinematic viscosity, ν = μ/ η (m ² /sec)	Speed of sound, a (m/sec)	Mean free path of molecules, λ (m)
(b) For day only										
80,000	240.0	0.3256	3151×10 ⁻⁸	4726×10 ⁻⁹	3782×10 ⁻⁸	4635×10 ⁻⁸	1.568×10 ⁻⁶	0.3318	310.6	1.95×10 ⁻³
81,000	240.0	0.2826	2733	4050	3280	3261	1.568	0.3825	312.5	2.25
82,000	240.0	0.2450	2378	3493	3246	3268	1.568	0.4111	314.2	2.58
83,000	240.0	0.2125	2070	3084	2468	2451	1.568	0.5085	316.5	2.97
84,000	243.6	0.1855	1866	2561	2049	2012	1.568	0.6211	320.8	3.45
85,000	247.3	0.1634	1682	2188	1751	1975	1.568	0.7448	325.2	4.00
86,000	250.0	0.1435	1589	1874	1500	1638	1.568	0.8682	330.6	4.62
87,000	254.6	0.1265	1424	1612	1290	1587	1.568	1.0211	333.9	5.32
88,000	258.2	0.1115	1082	1391	1113	1367	1.568	1.1971	336.3	6.11
89,000	263.9	0.09908	959.0	1204	963.7	1161	1.568	1.4000	342.7	6.99
90,000	265.5	0.08810	852.7	1046	837.1	1026	1.568	1.629	347.1	7.97
91,000	269.2	0.07850	759.7	910.9	728.9	893.2	1.568	1.892	351.5	9.07
92,000	272.8	0.07016	679.0	795.7	636.7	780.3	1.568	2.189	355.4	10.3
93,000	276.5	0.06285	608.3	697.0	557.8	683.6	1.568	2.526	360.4	11.6
94,000	280.1	0.05643	546.1	611.9	489.7	600.1	1.568	2.907	364.8	13.1
95,000	283.8	0.05079	491.6	638.8	431.1	528.4	1.568	3.335	369.2	14.8
96,000	287.4	0.04584	443.7	675.8	389.7	466.6	1.568	3.816	373.7	16.6
97,000	291.1	0.04144	401.1	621.0	336.9	413.9	1.568	4.357	378.1	18.6
98,000	294.7	0.03756	363.5	373.5	298.9	366.3	1.568	4.980	382.6	20.7
99,000	298.4	0.03410	330.1	332.0	265.7	325.6	1.568	5.633	387.1	23.1
100,000	302.0	0.03102	300.2	266.8	236.7	280.1	1.568	6.383	391.5	25.7
101,000	305.7	0.02827	273.6	213.1	201.2	1.568	7.157	393.9	28.6	
102,000	309.3	0.02579	249.6	204.1	192.1	235.2	1.568	8.013	396.2	31.7
103,000	313.0	0.02355	227.9	196.7	173.1	222.5	1.568	8.959	398.6	35.1
104,000	315.6	0.02153	208.4	195.8	159.7	192.0	1.568	10.000	400.9	38.9
105,000	319.3	0.01970	190.7	177.2	148.8	173.7	1.568	11.16	403.2	43.0
106,000	323.0	0.01805	174.7	160.5	136.1	162.7	1.568	12.42	405.5	47.5
107,000	326.7	0.01659	160.2	142.9	116.1	142.7	1.568	13.82	407.7	52.3
108,000	331.4	0.01535	147.0	132.1	105.7	129.5	1.568	15.36	410.0	57.7
109,000	334.9	0.01385	135.1	120.0	96.03	117.7	1.568	17.04	412.3	63.5
110,000	338.5	0.01263	124.2	109.2	87.35	107.1	1.568	18.89	414.5	69.8
111,000	342.2	0.01181	114.3	99.40	79.54	97.45	1.568	20.79	416.7	75.8
112,000	345.8	0.01088	105.3	90.60	72.50	88.85	1.568	22.13	418.9	84.0
113,000	349.5	0.01003	97.08	82.66	66.14	81.05	1.568	22.11	421.1	92.1
114,000	353.1	0.009255	89.58	75.9	60.40	74.02	1.568	22.21	423.3	101
115,000	356.8	0.008588	82.73	69.00	55.21	67.66	1.568	23.10	425.5	110
116,000	360.4	0.007900	76.46	63.13	50.51	61.91	1.568	24.25	427.7	121
117,000	364.1	0.007308	70.73	57.81	46.26	56.59	1.568	25.40	429.8	132
118,000	367.7	0.006765	65.47	52.98	42.40	51.95	1.568	26.55	432.0	144
119,000	371.4	0.006267	60.66	48.80	38.89	47.66	1.568	27.70	434.1	157
120,000	375.0	0.005810	56.24	44.62	35.71	43.76	1.568	49.92	436.3	171
(c) For night only										
80,000	240.0	0.3256	3151×10 ⁻⁸	4726×10 ⁻⁹	3782×10 ⁻⁸	4635×10 ⁻⁸	1.568×10 ⁻⁶	0.3318	310.6	1.95×10 ⁻³
81,000	240.0	0.2826	2733	4099	3280	4020	1.568	0.3825	312.5	2.25
82,000	240.0	0.2450	2371	3555	3246	3266	1.568	0.4111	314.2	2.58
83,000	240.0	0.2125	2056	3084	2467	3024	1.568	0.5085	316.5	2.99
84,000	243.6	0.1845	1785	2637	2110	2586	1.568	0.6021	318.9	3.49
85,000	247.3	0.1605	1553	2261	1809	2217	1.568	0.7110	315.3	4.07
86,000	250.9	0.1399	1354	1943	1554	1905	1.568	0.8376	317.6	4.74
87,000	254.6	0.1222	1183	1573	1338	1640	1.568	0.9834	319.9	5.51
88,000	258.2	0.1070	1036	1443	1155	1415	1.568	1.154	322.2	6.38
89,000	261.9	0.09383	908.1	1248	998.6	1224	1.568	1.350	324.4	7.38
90,000	265.5	0.08243	797.8	1081	865.3	1060	1.568	1.576	326.7	8.52
91,000	269.2	0.07234	702.1	928.6	720.2	928.5	1.568	1.832	328.9	9.81
92,000	272.8	0.06295	627.6	616.5	593.3	600.5	1.568	2.172	331.4	11.3
93,000	276.5	0.05427	542.8	524.2	492.3	509.1	1.568	2.564	333.5	12.86
94,000	280.1	0.04625	463.3	521.1	434.6	529.1	1.568	3.03	335.5	14.00
95,000	283.8	0.04042	380.0	479.6	380.7	446.6	1.568	3.516	337.7	17.00
96,000	287.4	0.03426	307.7	417.5	334.6	409.4	1.568	4.093	339.9	19.4
97,000	291.1	0.03048	237.7	347.5	324.6	400.4	1.568	4.670	342.0	22.1
98,000	294.7	0.03105	206.5	367.0	302.6	359.3	1.568	5.048	344.2	23.5
99,000	298.4	0.02707	207.0	323.0	258.5	326.8	1.568	5.790	346.3	26.5
100,000	302.0	0.02469	239.0	264.8	227.9	279.3	1.568	6.630	348.4	32.3
101,000	305.7	0.02207	213.6	251.5	201.2	246.6	1.568	7.579	350.5	36.6
102,000	309.3	0.01975	191.1	222.4	178.0	218.1	1.568	8.651	352.6	41.4
103,000	313.0	0.01770	171.3	197.0	157.6	193.1	1.568	9.859	354.7	46.8
104,000	316.6	0.01588	153.6	174.7	139.8	171.3	1.568	11.22	356.7	52.7
105,000	320.3	0.01426	138.0	155.1	124.1	152.1	1.568	12.74	358.8	59.4
106,000	323.9	0.01284	124.2	136.2	109.0	133.5	1.568	14.64	363.9	66.7
107,000	327.6	0.01158	112.1	119.8	95.89	117.5	1.568	16.78	369.0	74.8
108,000	331.2	0.01048	101.4	105.8	84.62	103.7	1.568	19.18	374.1	83.6
109,000	334.9	0.009501	91.95	93.60	74.90	91.79	1.568	21.85	379.2	93.2
110,000	338.5	0.008636	83.58	83.06	66.47	81.46	1.568	24.83	384.3	104
111,000	342.2	0.007887	76.14	73.90	59.13	72.47	1.568	26.79	389.4	115
112,000	345.8	0.007183	69.32	66.91	52.74	64.63	1.568	28.98	394.6	127
113,000	349.5	0.006573	63.82	58.83	47.16	57.73	1.568	31.13	399.3	141
114,000	353.1	0.006026	58.92	52.80	42.20	52.78	1.568	32.93	404.9	155
115,000	356.8	0.005534	53.20	47.22	37.94	48.93	1.568	34.26	410.1	169
116,000	360.4	0.005091	49.20	42.66	34.78	43.83	1.568	35.62	415.2	187
117,000	364.1	0.004695	45.44	38.47	30.70	37.73	1.568	36.53	420.6	205
118,000	367.7	0.004339	41.97	34.77	27.82	34.92	1.568	38.14	425.8	224
119,000	371.4	0.004011	38.82	34.47	25.18	30.88	1.568	40.21	431.0	245
120,000	375.0	0.003718	35.98	26.55	22.85	28.00	1.568	43.63	436.3	267

¹The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE III.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY
CONSTANT VALUE OF GRAVITATIONAL FORCE—BRITISH ENGINEERING SYSTEM

Altitude, (ft)	Absolute temperature, T (°F abs.)	Pressure, (lb/ft ²)	Pressure ratio, P/P_0	Density, ρ (slugs/ft ³)	Density ratio, ρ/ρ_0	Specific weight, $w = P/g$ (lb/ft ³)	Coefficient of viscosity, $\mu = F/(lb \cdot sec/ft^2)$ (lb \cdot sec/ft ²)	Kinematic viscosity, $\nu = \mu/F$ (ft ² /sec)	Speed of sound, $c = F/\rho$ (ft/sec)	Mean free path of molecules, λ (ft)
(a) For both day and night										
53,000	392.4	118.8	561x10 ⁻⁵	1765x10 ⁻⁷	741x10 ⁻⁵	5872x10 ⁻⁶	2.961x10 ⁻⁷	0.001680	971.1	0.00226x10 ⁻³
55,000	392.4	113.2	5250	1681	7068	5107	2.961	0.001761	971.1	0.00232
57,000	392.4	107.9	5100	1602	6785	5155	2.961	0.001848	971.1	0.00239
58,000	392.4	103.9	4867	1527	6423	4914	2.961	0.001939	971.1	0.00247
59,000	392.4	98.09	4635	1456	6123	4808	2.961	0.002034	971.1	0.00255
60,000	392.4	92.32	4419	1386	5836	4766	2.961	0.002133	971.1	0.00263
61,000	392.4	86.16	4213	1324	5626	4726	2.961	0.002236	971.1	0.00271
62,000	392.4	80.03	4017	1262	5427	4680	2.961	0.002346	971.1	0.00278
63,000	392.4	73.97	3821	1203	5228	4634	2.961	0.002461	971.1	0.00285
64,000	392.4	67.96	3631	1147	5032	4580	2.961	0.002576	971.1	0.00292
65,000	392.4	61.97	3451	1094	4839	4529	2.961	0.002691	971.1	0.00299
66,000	392.4	55.97	3273	1042	4643	4479	2.961	0.002806	971.1	0.00306
67,000	392.4	50.00	3103	993.7	4479	4417	2.961	0.002921	971.1	0.00313
68,000	392.4	43.04	2937	947.1	4303	4347	2.961	0.003037	971.1	0.00320
69,000	392.4	36.17	2773	903.1	4150	4296	2.961	0.003153	971.1	0.00327
70,000	392.4	29.32	2619	3686	4066	4166	2.961	0.003268	971.1	0.00334
71,000	392.4	22.56	2463	3242	3926	4256	2.961	0.003386	971.1	0.00343
72,000	392.4	16.87	2317	2895	3784	4524	2.961	0.003506	971.1	0.00352
73,000	392.4	11.26	2275	2561	3674	4824	2.961	0.003626	971.1	0.00361
74,000	392.4	6.71	2236	2256	3571.2	5101	2.961	0.003746	971.1	0.00367
75,000	392.4	2.23	2197	1963	3472	5359	2.961	0.003866	971.1	0.00373
76,000	392.4	1.94	2161	1871	3386	5679	2.961	0.003986	971.1	0.00360
77,000	392.4	1.75	2125	1783	3306	5996	2.961	0.004106	971.1	0.00348
78,000	392.4	1.60	2091	1707	3227	6316	2.961	0.004226	971.1	0.00336
79,000	392.4	1.47	2056	1633	3149	6636	2.961	0.004346	971.1	0.00324
80,000	392.4	1.35	2021	1563	3073	6956	2.961	0.004466	971.1	0.00312
81,000	392.4	1.24	1986	1493	2995	7276	2.961	0.004586	971.1	0.00300
82,000	392.4	1.14	1951	1423	2916	7596	2.961	0.004706	971.1	0.00288
83,000	392.4	1.05	1917	1353	2836	7916	2.961	0.004826	971.1	0.00277
84,000	392.4	0.97	1882	1283	2756	8236	2.961	0.004946	971.1	0.00265
85,000	392.4	0.89	1847	1213	2676	8556	2.961	0.005066	971.1	0.00253
86,000	392.4	0.82	1812	1143	2596	8876	2.961	0.005186	971.1	0.00241
87,000	392.4	0.76	1777	1074	2516	9196	2.961	0.005306	971.1	0.00229
88,000	392.4	0.70	1742	1004	2436	9516	2.961	0.005426	971.1	0.00218
89,000	392.4	0.65	1707	934	2356	9836	2.961	0.005546	971.1	0.00206
90,000	392.4	0.60	1672	864	2276	10156	2.961	0.005666	971.1	0.00195
91,000	392.4	0.56	1637	794	2196	10476	2.961	0.005786	971.1	0.00184
92,000	392.4	0.52	1602	724	2116	10796	2.961	0.005906	971.1	0.00173
93,000	392.4	0.48	1567	654	2036	11116	2.961	0.006026	971.1	0.00162
94,000	392.4	0.44	1532	584	1956	11436	2.961	0.006146	971.1	0.00151
95,000	392.4	0.40	1497	514	1876	11756	2.961	0.006266	971.1	0.00140
96,000	392.4	0.36	1462	444	1796	12076	2.961	0.006386	971.1	0.00129
97,000	392.4	0.32	1427	374	1716	12396	2.961	0.006506	971.1	0.00118
98,000	392.4	0.28	1392	304	1636	12716	2.961	0.006626	971.1	0.00107
99,000	392.4	0.24	1357	234	1556	13036	2.961	0.006746	971.1	0.00096
100,000	392.4	0.21	1322	164	1476	13356	2.961	0.006866	971.1	0.00085
102,000	392.4	0.17	1287	94	1396	13676	2.961	0.006986	971.1	0.00074
104,000	392.4	0.14	1252	24	1316	14006	2.961	0.007106	971.1	0.00063
106,000	392.4	0.11	1217	14	1236	14336	2.961	0.007226	971.1	0.00052
108,000	392.4	0.08	1182	4	1156	14666	2.961	0.007346	971.1	0.00041
110,000	392.4	0.06	1147	1	1076	15006	2.961	0.007466	971.1	0.00030
112,000	392.4	0.04	1112	1	996	15336	2.961	0.007586	971.1	0.00020
114,000	392.4	0.03	1077	1	916	15666	2.961	0.007706	971.1	0.00010
116,000	392.4	0.02	1042	1	836	16006	2.961	0.007826	971.1	0.00009
118,000	392.4	0.01	1007	1	756	16336	2.961	0.007946	971.1	0.00008
120,000	392.4	0.00	972	1	676	16666	2.961	0.008066	971.1	0.00007
122,000	392.4	-0.02	937	1	596	17006	2.961	0.008186	971.1	0.00006
124,000	392.4	-0.04	892	1	516	17336	2.961	0.008306	971.1	0.00005
126,000	392.4	-0.06	847	1	436	17666	2.961	0.008426	971.1	0.00004
128,000	392.4	-0.08	802	1	356	18006	2.961	0.008546	971.1	0.00003
130,000	392.4	-0.10	757	1	276	18336	2.961	0.008666	971.1	0.00002
132,000	392.4	-0.12	712	1	196	18666	2.961	0.008786	971.1	0.00001
134,000	392.4	-0.14	667	1	116	19006	2.961	0.008906	971.1	0.00000
136,000	392.4	-0.16	622	1	36	19336	2.961	0.009026	971.1	0.00000
138,000	392.4	-0.18	577	1	176	19666	2.961	0.009146	971.1	0.00000
140,000	393.3	-0.21	532	1	97	20006	2.961	0.009266	971.1	0.00000
142,000	393.3	-0.24	487	1	17	20336	2.961	0.009386	971.1	0.00000
144,000	393.3	-0.27	442	1	37	20666	2.961	0.009506	971.1	0.00000
146,000	393.3	-0.30	397	1	57	21006	2.961	0.009626	971.1	0.00000
148,000	393.3	-0.33	352	1	77	21336	2.961	0.009746	971.1	0.00000
150,000	393.3	-0.36	307	1	97	21666	2.961	0.009866	971.1	0.00000
152,000	393.3	-0.39	262	1	117	22006	2.961	0.009986	971.1	0.00000
154,000	393.3	-0.42	217	1	137	22336	2.961	0.010106	971.1	0.00000
156,000	393.3	-0.45	172	1	157	22666	2.961	0.010226	971.1	0.00000
158,000	393.3	-0.48	127	1	177	23006	2.961	0.010346	971.1	0.00000
160,000	393.3	-0.51	82	1	197	23336	2.961	0.010466	971.1	0.00000
162,000	393.3	-0.54	37	1	217	23666	2.961	0.010586	971.1	0.00000
164,000	393.3	-0.57	12	1	237	24006	2.961	0.010706	971.1	0.00000
166,000	393.3	-0.60	1	1	257	24336	2.961	0.010826	971.1	0.00000
168,000	393.3	-0.63	1	1	277	24666	2.961	0.010946	971.1	0.00000
170,000	393.3	-0.66	1	1	297	25006	2.961	0.011066	971.1	0.00000
172,000	393.3	-0.69	1	1	317	25336	2.961	0.011186	971.1	0.00000
174,000	393.3	-0.72	1	1	337	25666	2.961	0.011306	971.1	0.00000
176,000	393.3	-0.75	1	1	357	26006	2.961	0.011426	971.1	0.00000
178,000	393.3	-0.78	1	1	377	26336	2.961	0.011546	971.1	0.00000
180,000	393.3	-0.81	1	1	397	26666	2.961	0.011666	971.1	0.00000
182,000	393.3	-0.84	1	1	417	27006	2.961	0.011786	971.1	0.00000
184,000	393.3	-0.87	1	1	437	27336	2.961	0.011906	971.1	0.00000
186,000	393.3	-0.90	1	1	457	27666	2.961	0.012026	971.1	0.00000
188,000	393.3	-0.93	1	1	477	28006	2.961	0.012146	971.1	0.00000
190,000	393.3	-0.96	1	1	497	28336	2.961	0.012266	971.1	0.00000
192,000	393.3	-0.99	1	1	517	28666	2.961	0.012386	971.1	0.00000
194,000	393.3	-0.102	1	1	537	29006	2.961			

TABLE III.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY
CONSTANT VALUE OF GRAVITATIONAL FORCE—BRITISH ENGINEERING SYSTEM—Continued

Altitude, ^b (ft)	Absolute temperature, ^a (°F abs.)	Pressure, ^P (lb/ft ²)	Pressure ratio, ^{P/P₀}	Density, ^P (slugs/ft ³)	Density ratio, $\sigma = \frac{P}{P_0}$	Specific weight, $\gamma = \frac{P}{\rho g}$ (lb/ft ³)	Coefficient of viscosity, μ (lb sec/ft ²) (l)	Kinematic viscosity, $\nu = \frac{\mu}{\rho}$ (ft ² /sec) (l)	Speed of sound, ^c (ft/sec)	Mean free path of molecules, λ (ft)
(b) For day only										
262,467	432.0	0.06669	3.151x10 ⁻⁵	89.93x10 ⁻⁹	3.782x10 ⁻⁵	2.893x10 ⁻⁶	3.212x10 ⁻⁷	3.572	1019	6.40x10 ⁻³
264,000	432.0	0.06241	2.949	83.75	3.522	2.695	3.212	3.835	1022	6.84
266,000	432.0	0.05724	2.705	76.33	3.210	2.456	3.212	4.208	1026	7.45
268,000	432.0	0.05257	2.484	69.65	2.929	2.241	3.212	4.612	1030	8.12
270,000	432.0	0.04829	2.282	63.59	2.674	2.046	3.212	5.051	1034	8.83
272,006	432.0	0.04438	2.097	58.07	2.442	1.868	3.212	5.531	1038	9.61
272,309	432.0	0.04381	2.070	57.26	2.408	1.842	3.212	5.610	1038	9.74
274,000	435.4	0.04082	1.929	52.67	2.215	1.695	3.232	6.136	1046	10.5
276,000	439.4	0.03760	1.776	47.77	2.009	1.537	3.257	6.818	1054	11.5
278,000	443.4	0.03469	1.638	43.42	1.826	1.397	3.282	7.559	1063	12.6
280,000	447.4	0.03200	1.512	39.45	1.659	1.269	3.306	8.380	1072	13.8
282,000	451.4	0.02956	1.397	35.91	1.510	1.155	3.331	9.273	1081	14.1
284,000	455.4	0.02736	1.293	32.74	1.377	1.053	3.355	10.25	1089	14.4
286,000	459.4	0.02535	1.198	29.89	1.257	0.9616	3.379	11.30	1098	17.9
288,000	463.4	0.02351	1.111	27.32	1.149	0.8791	3.403	12.46	1107	19.5
290,000	467.4	0.02184	1.032	25.02	1.052	0.8048	3.427	13.70	1116	21.1
292,000	471.4	0.02029	0.9588	22.91	0.9635	0.7371	3.451	15.06	1124	22.9
294,000	475.4	0.01888	0.8920	21.01	0.8837	0.6761	3.475	16.54	1133	24.9
296,000	479.4	0.01759	0.8310	19.30	0.8117	0.6210	3.499	18.13	1142	26.9
298,000	483.4	0.01639	0.7746	17.74	0.7450	0.5707	3.523	19.86	1151	29.1
300,000	487.4	0.01530	0.7228	16.32	0.6865	0.5252	3.546	21.73	1160	31.5
302,000	491.4	0.01428	0.6750	15.03	0.6322	0.4837	3.569	23.75	1169	34.0
304,000	495.4	0.01326	0.6314	13.87	0.5833	0.4453	3.593	25.98	1177	36.6
306,000	499.4	0.01250	0.5908	12.80	0.5384	0.4119	3.616	28.25	1186	39.4
308,000	503.4	0.01170	0.5521	11.82	0.4972	0.3804	3.639	30.79	1195	42.5
310,000	507.4	0.01098	0.5185	10.94	0.4599	0.3519	3.662	33.47	1204	45.7
312,000	511.5	0.01030	0.4886	10.13	0.4259	0.3258	3.685	36.28	1213	49.0
314,000	515.5	0.009671	0.4576	9.395	0.3947	0.3020	3.708	39.21	1222	52.4
316,000	519.5	0.009091	0.4296	8.705	0.3661	0.2801	3.731	42.06	1231	56.4
318,000	523.5	0.008550	0.4040	8.082	0.3399	0.2600	3.754	46.45	1240	60.5
320,000	527.5	0.008050	0.3804	7.509	0.3158	0.2416	3.777	50.30	1248	64.7
322,000	531.5	0.007585	0.3584	6.984	0.2937	0.2247	3.799	54.46	1257	69.2
324,000	535.5	0.007153	0.3380	6.504	0.2735	0.2092	3.822	58.75	1266	73.9
326,000	539.5	0.006744	0.3187	6.054	0.2546	0.1948	3.844	63.50	1275	79.0
328,000	543.5	0.006358	0.3009	5.645	0.2374	0.1816	3.867	68.48	1284	84.3
328,083	543.6	0.006353	0.3002	5.628	0.2357	0.1811	3.887	68.71	1285	84.5
330,000	547.5	0.006012	0.2811	5.288	0.2224	0.1701	3.889	73.54	1289	89.9
332,000	551.5	0.005686	0.2687	4.965	0.2088	0.1597	9.911	78.77	1294	95.8
334,000	555.5	0.005377	0.2521	4.661	0.1950	0.1500	9.933	84.38	1298	102
336,000	559.5	0.005087	0.2404	4.380	0.1812	0.1409	9.955	90.30	1303	109
338,000	563.5	0.004812	0.2274	4.114	0.1730	0.1324	3.977	95.67	1308	116
340,000	567.5	0.004556	0.2153	3.866	0.1626	0.1244	3.999	103.4	1312	123
342,000	571.5	0.004315	0.2039	3.635	0.1529	0.1170	4.021	110.5	1317	131
344,000	575.5	0.004091	0.1933	3.424	0.1440	0.1102	4.043	118.5	1322	139
346,000	579.5	0.003875	0.1831	3.220	0.1354	0.1036	4.065	126.21	1326	148
348,000	583.5	0.003674	0.1736	3.032	0.1275	0.09755	4.086	134.8	1331	157
350,000	587.5	0.003486	0.1647	2.858	0.1202	0.09196	4.108	143.7	1335	167
352,000	591.5	0.0033306	0.1562	2.692	0.1132	0.08660	4.129	153.4	1340	177
354,000	595.5	0.0031336	0.1482	2.537	0.1067	0.08163	4.151	163.6	1344	188
356,000	599.5	0.002978	0.1407	2.392	0.1006	0.07697	4.172	174.4	1349	199
358,000	603.5	0.002829	0.1337	2.258	0.09495	0.07264	4.193	185.7	1353	211
360,000	607.5	0.002690	0.1271	2.132	0.08967	0.06860	4.214	197.7	1358	223
362,000	611.5	0.002556	0.1208	2.013	0.08466	0.06477	4.236	210.4	1362	236
364,000	615.5	0.002429	0.1148	1.901	0.07994	0.06116	4.257	223.9	1367	250
366,000	619.5	0.002321	0.1092	1.795	0.07554	0.05779	4.278	238.2	1371	265
368,000	623.6	0.002199	0.1039	1.658	0.07142	0.05451	4.299	253.2	1376	280
370,000	627.6	0.002092	0.0987	1.566	0.06753	0.05166	4.319	268.9	1380	296
372,000	631.6	0.001992	0.09411	1.519	0.06387	0.04886	4.340	285.7	1384	313
374,000	635.6	0.001897	0.08982	1.437	0.06044	0.04644	4.361	303.5	1389	331
376,000	639.6	0.001806	0.08536	1.360	0.05720	0.04376	4.382	322.6	1393	350
378,000	643.6	0.001721	0.08133	1.288	0.05416	0.04144	4.402	341.8	1398	370
380,000	647.6	0.001640	0.07751	1.220	0.05130	0.03925	4.423	362.5	1402	390
382,000	651.6	0.001564	0.07390	1.156	0.04861	0.03719	4.443	384.3	1406	411
384,000	655.6	0.001492	0.07049	1.096	0.04609	0.03526	4.464	407.3	1411	434
386,000	659.6	0.001423	0.06724	1.039	0.04369	0.03343	4.484	431.6	1415	458
388,000	663.6	0.001358	0.06417	0.986	0.04145	0.03171	4.504	457.0	1419	483
390,000	667.6	0.001296	0.06126	0.9352	0.03933	0.03009	4.525	483.9	1423	509
392,000	671.6	0.001237	0.05847	0.8872	0.03731	0.02854	4.545	512.3	1426	536
393,700	675.0	0.001190	0.05624	0.8491	0.03571	0.02732	4.562	537.3	1431	560

¹The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE III.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN ARBITRARY
CONSTANT VALUE OF GRAVITATIONAL FORCE—BRITISH ENGINEERING SYSTEM—Concluded

Altitude, h (ft)	Absolute tempera- ture, T (°F abs.)	Pressure, P (lb/ft ²)	Pressure ratio, P/P ₀	Density, P (slugs/ft ³)	Density ratio, σ = P/P ₀	Specific Weight, w = gP (lb/ft ³)	Coefficient of viscosity μ (lb-sec/ft ²) (1)	Kinematic viscosity, ν = μ/w (ft ² /sec) (1)	Speed of sound, a (ft/sec)	Mean free path of molecules, λ (ft)
(c) For night only										
262,467	432.0	0.06669	3.151x10 ⁻⁵	89.93x10 ⁻⁹	3.782x10 ⁻⁵	2.893x10 ⁻⁶	3.212x10 ⁻⁷	3.572	1019	6.40x10 ⁻³
264,000	432.0	0.06239	2.948	84.13	3.538	2.707	3.212	3.818	1019	6.8k
266,000	432.0	0.05720	2.703	77.14	3.244	2.482	3.212	4.164	1019	7.16
268,000	432.0	0.05246	2.479	70.74	2.975	2.276	3.212	4.541	1019	8.13
270,000	432.0	0.04810	2.273	64.87	2.728	2.087	3.212	4.951	1016	8.87
272,000	432.0	0.04410	2.084	59.47	2.501	1.913	3.212	5.401	1019	9.67
272,309	432.0	0.04351	2.056	58.67	2.467	1.887	3.212	5.475	1019	9.80
274,000	435.4	0.04044	1.911	54.10	2.275	1.741	3.232	2.974	1023	10.6
276,000	439.4	0.03712	1.754	49.20	2.069	1.583	3.297	6.620	1028	11.7
278,000	443.4	0.03408	1.611	44.80	1.884	1.441	3.282	7.326	1032	12.8
280,000	447.4	0.03134	1.481	40.80	1.716	1.313	3.306	8.103	1037	14.1
282,000	451.4	0.02854	1.363	37.24	1.566	1.198	3.331	8.945	1042	15.5
284,000	455.4	0.02656	1.255	33.98	1.429	1.093	3.355	9.873	1046	16.9
286,000	459.4	0.02446	1.156	31.01	1.304	0.9976	3.379	10.90	1051	18.5
288,000	463.4	0.02256	1.066	28.34	1.192	0.9120	3.403	12.01	1055	20.3
290,000	467.4	0.02081	0.9832	25.92	1.090	0.8339	3.427	13.22	1060	22.2
292,000	471.4	0.01921	0.9079	23.74	0.9984	0.7638	3.451	14.54	1064	24.2
294,000	475.4	0.01774	0.8384	21.74	0.9142	0.6994	3.475	15.98	1069	26.5
296,000	479.4	0.01640	0.7748	19.92	0.8378	0.6110	3.499	17.57	1073	28.9
298,000	483.4	0.01517	0.7163	18.28	0.7887	0.5881	3.523	19.27	1078	31.5
300,000	487.4	0.01406	0.66643	16.80	0.7065	0.5405	3.546	21.11	1082	34.2
302,000	491.4	0.01302	0.6151	15.43	0.5689	0.4964	3.569	23.13	1087	37.3
304,000	495.4	0.01206	0.5699	14.18	0.5063	0.4562	3.593	25.34	1091	40.6
306,000	499.4	0.01119	0.5286	13.05	0.5887	0.4196	3.616	27.71	1096	44.1
308,000	503.4	0.01038	0.4906	12.01	0.5052	0.3865	3.639	30.30	1100	47.9
310,000	507.4	0.009442	0.4586	11.07	0.4854	0.3561	3.662	33.08	1104	52.0
312,000	511.5	0.008558	0.4233	10.20	0.4290	0.3282	3.685	36.13	1109	56.4
314,000	515.5	0.008327	0.3935	9.409	0.3957	0.3027	3.708	39.41	1113	61.1
316,000	519.5	0.007745	0.3680	8.886	0.3653	0.2795	3.731	42.95	1117	66.2
318,000	523.5	0.007210	0.3407	8.023	0.3374	0.2581	3.754	46.79	1122	71.7
320,000	527.5	0.006711	0.3171	7.410	0.3116	0.2384	3.777	50.97	1126	77.6
322,000	531.5	0.006253	0.2955	6.853	0.2882	0.2205	3.799	55.44	1130	83.9
324,000	535.5	0.005826	0.2753	6.337	0.2665	0.2039	3.822	60.31	1134	90.8
326,000	539.5	0.005437	0.2569	5.871	0.2469	0.1889	3.844	65.47	1139	98.0
328,000	543.5	0.005073	0.2397	5.436	0.2285	0.1749	3.867	71.14	1143	106
330,000	547.5	0.004736	0.2238	5.039	0.2119	0.1621	3.889	77.18	1147	114
332,000	551.5	0.004423	0.2090	4.673	0.1865	0.1503	3.911	83.69	1151	123
334,000	555.5	0.004133	0.1853	4.335	0.1823	0.1395	3.933	90.73	1155	133
336,000	559.5	0.003864	0.1826	4.023	0.1692	0.1294	3.955	96.31	1160	143
338,000	563.5	0.003617	0.1709	3.738	0.1572	0.1203	3.977	106.4	1164	154
340,000	567.5	0.003384	0.1599	3.474	0.1451	0.1118	3.999	115.1	1168	166
342,000	571.5	0.003166	0.1496	3.227	0.1357	0.1038	4.021	124.6	1172	178
344,000	575.5	0.002967	0.1402	3.003	0.1263	0.09663	4.043	134.6	1176	192
346,000	579.5	0.002920	0.1380	2.951	0.1241	0.09494	4.048	137.2	1177	195
348,000	583.5	0.002781	0.1314	2.777	0.1168	0.08936	4.065	146.4	1185	206
350,000	587.5	0.002453	0.1159	2.376	0.09992	0.07644	4.108	159.1	1195	221
352,000	591.5	0.002305	0.1089	2.199	0.08248	0.07075	4.129	172.9	1205	237
354,000	595.5	0.002169	0.1025	2.039	0.08575	0.06569	4.151	187.0	1215	253
356,000	599.5	0.002041	0.09646	1.891	0.07921	0.06083	4.172	203.0	1226	271
358,000	603.5	0.001924	0.09090	1.756	0.07383	0.05748	4.193	220.0	1236	290
360,000	607.5	0.001815	0.08576	1.632	0.06864	0.05251	4.214	238.8	1246	310
362,000	611.5	0.001714	0.08098	1.519	0.06388	0.04887	4.236	278.9	1267	353
364,000	615.5	0.001618	0.07648	1.414	0.05947	0.04550	4.257	301.1	1277	376
366,000	619.5	0.001531	0.07238	1.319	0.05546	0.04243	4.278	324.3	1287	400
368,000	623.5	0.001449	0.06848	1.231	0.05175	0.03959	4.299	349.2	1297	425
370,000	627.5	0.001373	0.06488	1.149	0.04834	0.03698	4.319	375.9	1308	451
372,000	631.5	0.001302	0.06151	1.075	0.04520	0.03458	4.340	403.7	1318	479
374,000	635.5	0.001235	0.05836	1.006	0.04229	0.03235	4.361	433.5	1328	508
376,000	639.5	0.001172	0.05537	0.9409	0.03957	0.03027	4.382	465.7	1339	539
378,000	643.5	0.001113	0.05260	0.8817	0.03708	0.02837	4.402	499.3	1349	571
380,000	647.5	0.001058	0.05000	0.8268	0.03477	0.02660	4.423	535.0	1359	604
382,000	651.5	0.001007	0.04757	0.7761	0.03264	0.02497	4.443	572.5	1370	639
384,000	655.5	0.0009582	0.04528	0.7283	0.03065	0.02345	4.464	612.5	1381	676
386,000	659.5	0.0009127	0.04313	0.6851	0.02881	0.02204	4.484	654.5	1391	714
388,000	663.5	0.0008702	0.04132	0.6444	0.02710	0.02073	4.504	698.9	1401	754
390,000	667.5	0.0008296	0.03920	0.6064	0.02550	0.01951	4.525	746.2	1412	795
392,000	671.5	0.0007917	0.03741	0.5712	0.02402	0.01838	4.545	795.7	1422	838
393,700	675.0	0.0007614	0.03598	0.5434	0.02285	0.01748	4.562	839.5	1431	875

¹The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLES IV AND V

PROPERTIES OF THE UPPER ATMOSPHERE
FOR TENTATIVE STANDARD TEMPERATURES
BASED ON AN INVERSE SQUARE VARIATION
OF GRAVITATIONAL FORCE

The following set of two tables (tables IV and V) does not constitute a consistent extension of the standard tables for the lower atmosphere (NACA Rep. No. 218) but takes into account the inverse square law of gravitational attraction and, consequently, the values in these tables are more accurate than those in tables II and III.

NATIONAL ADVISORY
COMMITTEE FOR AERONAUTICS.

TABLE IV.—PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN

TABLE IV. — PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN INVERSE SQUARE VARIATION OF GRAVITATIONAL FORCE — METRIC ENGINEERING SYSTEM — Concluded

Altitude, h (m)	Absolute tempera- ture, T (°K)	Pressure, P (kg/m ²)	Pressure ratio, P/P ₀	Density, ρ (kg-sec ²) m ⁻⁴	Density ratio, $\sigma = \frac{\rho}{\rho_0}$	Specific weight, $w = \frac{SP}{\rho}$ (kg/m ³)	Coefficient of viscosity, μ (kg-sec) m ²	Kinematic viscosity, $\nu = \frac{\mu}{P}$ (m ² /sec)	Speed of sound, U (m/sec)	Mean free path of molecules, λ (m)
(b) For day only										
80,000	240.0	0.3675	3557×10^{-8}	5334×10^{-9}	4268×10^{-8}	5102×10^{-8}	1.568×10^{-6}	0.2940	310.6	1.68×10^{-3}
81,000	240.0	0.3190	3096	4508	3680	4395	1.568	0.3411	310.6	1.93
82,000	240.0	0.2793	2703	3970	3177	5758	1.568	0.3926	310.6	2.22
83,000	240.0	0.2439	2361	3432	2744	5850	1.568	0.4568	310.6	2.54
84,000	243.6	0.2136	2067	2931	2345	5800	1.568	0.5415	310.6	2.94
85,000	247.3	0.1877	1817	2613	2011	5300	1.567	0.6394	310.6	3.39
86,000	250.0	0.1653	1600	2160	1729	2062	1.567	0.7329	310.6	3.91
87,000	254.6	0.1462	1415	1864	1452	1779	1.566	0.8827	310.6	4.48
88,000	258.2	0.1297	1285	1614	1292	1540	1.566	1.031	310.6	5.12
89,000	261.9	0.1153	1176	1402	1122	1337	1.565	1.202	310.6	5.84
90,000	265.5	0.1029	995.6	1222	977.5	1165	1.704	1.396	347.1	6.64
91,000	269.2	0.09195	890.0	1067	854.0	1017	1.723	1.614	351.5	7.52
92,000	272.8	0.08244	797.9	925.1	748.3	801.0	1.742	1.862	352.0	8.50
93,000	276.5	0.07408	717.0	821.5	687.3	766.8	1.760	2.143	356.0	9.59
94,000	280.1	0.06666	615.7	723.6	579.0	660.5	1.779	2.450	360.0	10.8
95,000	283.8	0.06023	585.0	628.9	569.0	605.5	1.797	2.804	369.2	12.1
96,000	287.4	0.05453	527.8	562.0	512.0	547.0	1.815	3.203	373.7	13.5
97,000	291.1	0.04945	475.6	502.2	461.0	498.0	1.834	3.693	378.0	15.1
98,000	294.7	0.04494	432.0	446.9	428.1	459.0	1.852	4.145	382.6	16.8
99,000	298.4	0.04093	390.1	398.5	316.0	370.9	1.870	4.694	387.1	18.7
100,000	302.0	0.03734	361.4	356.0	284.9	338.4	1.888	5.303	391.5	20.1
101,000	305.7	0.03412	330.2	321.4	257.2	305.5	1.906	6.288	393.9	21.4
102,000	309.3	0.03122	302.1	290.6	232.6	276.1	1.924	6.616	396.3	22.8
103,000	313.0	0.02859	276.7	263.1	210.5	249.3	1.941	6.315	398.9	24.0
104,000	315.6	0.02621	253.7	238.4	190.8	226.4	1.959	6.210	400.3	25.9
105,000	320.3	0.02406	238.8	216.3	173.1	205.3	1.976	6.120	403.3	27.1
106,000	323.9	0.02210	215.9	196.5	157.2	186.4	1.994	6.041	405.3	28.5
107,000	327.6	0.02032	196.7	178.7	143.0	165.0	2.011	5.974	407.7	29.8
108,000	331.2	0.01870	187.0	162.7	136.2	154.0	2.028	5.910	410.0	31.3
109,000	334.9	0.01723	166.8	148.2	116.2	140.5	2.045	5.879	412.3	32.7
110,000	338.5	0.01589	153.8	135.2	108.2	128.1	2.062	5.824	415.5	34.4
111,000	342.2	0.01465	141.9	123.5	98.79	117.0	2.079	5.783	418.7	36.2
112,000	345.8	0.01355	131.1	112.8	90.29	106.9	2.096	5.753	420.9	38.2
113,000	349.5	0.01252	121.2	103.2	82.69	97.75	2.113	20.45	421.1	40.6
114,000	353.1	0.01159	112.9	94.55	82.45	89.00	2.130	22.51	423.3	43.0
115,000	356.8	0.01074	103.9	96.27	80.74	82.00	2.148	24.75	426.3	44.8
116,000	360.4	0.009947	99.30	79.50	75.21	75.21	2.166	26.93	429.3	47.4
117,000	364.1	0.009227	89.30	73.00	68.41	70.93	2.184	29.83	429.3	50.1
118,000	367.7	0.008565	82.30	67.10	63.43	65.33	2.201	32.71	432.0	52.0
119,000	371.4	0.007958	77.02	62.72	59.36	61.33	2.219	35.62	434.1	54.9
120,000	375.0	0.007398	71.60	56.82	54.46	55.67	2.227	39.20	436.3	57.9
(c) For night only										
80,000	240.0	0.3675	3557×10^{-8}	5334×10^{-9}	4268×10^{-8}	5102×10^{-8}	1.568×10^{-6}	0.2940	310.6	1.68×10^{-3}
81,000	240.0	0.3190	3096	4508	3713	4139	1.568	0.3377	310.6	1.93
82,000	240.0	0.2793	2695	4041	3233	3863	1.568	0.3879	310.6	2.22
83,000	240.0	0.2424	2346	3518	2615	3361	1.568	0.4458	310.6	2.55
84,000	243.6	0.2112	2044	3020	2415	2885	1.568	0.5269	310.6	2.97
85,000	247.3	0.1844	1785	2598	2079	2481	1.567	0.6189	310.6	3.45
86,000	250.9	0.1613	1562	2240	1793	2138	1.567	0.7265	310.6	4.00
87,000	254.6	0.1415	1369	1936	1549	1847	1.565	0.8400	310.6	4.63
88,000	258.2	0.1248	1203	1675	1341	1599	1.566	0.9930	310.6	5.34
89,000	261.9	0.1094	1058	1455	1164	1387	1.565	1.153	310.6	6.16
90,000	265.5	0.09640	933.0	1265	1012	1206	1.704	1.347	326.7	7.08
91,000	269.2	0.08515	824.1	1101	881.1	1050	1.723	1.564	328.9	8.12
92,000	272.8	0.07533	729.1	951.8	769.6	916.4	1.742	1.811	331.4	9.31
93,000	276.5	0.06676	645.1	841.1	673.1	801.2	1.760	2.093	333.4	10.6
94,000	280.1	0.05926	573.5	737.0	589.7	701.8	1.779	2.414	335.5	12.1
95,000	283.8	0.05269	509.9	646.7	517.5	615.6	1.798	2.780	337.5	13.8
96,000	287.4	0.04661	451.0	568.5	454.0	511.1	1.816	3.195	339.9	15.7
97,000	291.1	0.04183	405.9	500.6	400.5	476.3	1.834	3.664	342.0	17.9
98,000	294.7	0.03736	361.5	441.5	353.5	420.0	1.852	4.196	344.2	20.2
99,000	298.4	0.03341	323.3	390.0	312.1	370.9	1.870	4.795	346.3	22.9
100,000	302.0	0.02992	289.5	345.0	276.1	328.0	1.888	5.472	348.4	25.9
101,000	305.7	0.02683	256.7	305.8	247.4	290.6	1.906	6.233	350.5	28.2
102,000	309.3	0.02409	233.2	271.3	217.1	257.8	1.924	7.090	352.6	30.9
103,000	313.0	0.02165	209.7	241.1	192.9	229.0	1.942	8.052	354.7	37.0
104,000	316.6	0.01950	188.8	214.5	171.6	203.7	1.959	9.130	356.7	41.6
105,000	320.3	0.01758	170.2	191.2	153.0	181.8	1.976	10.34	358.0	46.6
106,000	324.0	0.01588	153.7	168.4	134.8	159.8	1.994	11.84	360.0	52.2
107,000	327.6	0.01438	139.1	148.7	119.0	141.0	2.011	13.52	362.0	56.3
108,000	331.2	0.01305	126.3	131.7	105.4	124.8	2.028	15.41	374.1	64.9
109,000	334.9	0.01187	114.9	116.9	93.57	110.8	2.045	17.49	379.2	72.1
110,000	338.5	0.01082	104.8	104.1	83.30	98.63	2.062	19.81	384.3	79.9
111,000	342.2	0.009890	95.72	92.90	74.33	87.98	2.079	22.38	389.4	88.4
112,000	345.8	0.009059	87.68	83.11	66.50	78.70	2.095	25.92	394.8	97.5
113,000	349.5	0.008315	80.47	74.55	59.65	70.56	2.113	28.34	399.8	107
114,000	353.1	0.007546	74.00	66.99	53.60	63.40	2.129	31.76	404.9	118
115,000	356.8	0.007042	68.15	60.33	48.28	57.09	2.145	35.57	410.1	129
116,000	360.4	0.006499	62.90	58.44	43.56	53.49	2.162	38.72	415.3	141
117,000	364.1	0.006009	58.16	49.24	39.40	46.55	2.179	41.26	420.6	154
118,000	367.7	0.005567	53.88	44.63	35.71	42.18	2.195	44.18	425.8	168
119,000	371.4	0.005164	49.98	40.50	32.41	38.26	2.211	47.58	431.0	183
120,000	375.0	0.004800	45.45	36.86	29.50	34.82	2.227	50.42	436.3	199

¹The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE V... PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN
INVERSE SQUARE VARIATION OF GRAVITATIONAL FORCE — BRITISH ENGINEERING SYSTEM

Altitude, (ft)	Absolute tem- pera- ture, T (°F abs.)	Pressure, (lb/ft ²)	Pressure ratio, $\frac{P}{P_0}$	Density, ρ (slugs/ft ³)	Density ratio, $\rho = \frac{\rho}{\rho_0}$	Specific weight, γ = ρg (lb/ft ³)	Coefficient of viscosity, μ (lb·sec/ft ²)	Kinematic viscosity, $\nu = \frac{\mu}{\rho}$ (ft ² /sec)	Speed of sound, (ft/sec)	Mean free path of molecules, λ (ft)
(a) For both day and night										
64,000	392.4	119.9	5054×10 ⁻⁵	1779×10 ⁻⁷	7483×10 ⁻⁵	5690×10 ⁻⁶	2.961×10 ⁻⁷	0.00165	971.1	0.00321×10 ⁻³
65,000	392.4	117.3	5402	1657	7137	5126	2.961	0.001745	971.1	0.00337
67,000	392.4	109.0	5151	1616	6805	5173	2.961	0.001830	971.1	0.00353
68,000	392.4	104.0	4915	1543	6261	4523	2.961	0.001949	971.1	0.00370
69,000	392.4	99.12	4684	1474	6138	4703	2.961	0.00203	971.1	0.00388
70,000	392.4	94.53	4467	1403	5901	4486	2.961	0.002110	971.1	0.00407
71,000	392.4	80.17	4261	1359	5629	4277	2.961	0.002211	971.1	0.00427
72,000	392.4	70.86	4063	1317	5376	4075	2.961	0.002313	971.1	0.00446
73,000	392.4	68.86	3926	1279	5119	3869	2.961	0.002413	971.1	0.00469
74,000	392.4	78.19	3696	1236	4881	3708	2.961	0.00250	971.1	0.00492
75,000	392.4	77.4	3524	1197	4656	3537	2.961	0.002675	971.1	0.00516
76,000	392.4	71.13	3361	1095	4410	3372	2.961	0.002804	971.1	0.00541
77,000	392.4	67.76	3209	1048	4175	3261	2.961	0.00293	971.1	0.00567
78,000	392.4	67.26	3067	1007	3935	3026	2.961	0.003058	971.1	0.00594
79,000	392.4	61.59	2915	915.7	3681	2924	2.961	0.003234	971.1	0.00623
80,000	392.4	58.85	2780	875.4	3573	2783	2.961	0.003390	971.1	0.00654
81,000	392.4	56.16	2647	834.7	3502	2829	2.961	0.003556	971.1	0.00686
82,000	392.4	53.50	2516	794.2	3430	2853	2.961	0.003726	971.1	0.00719
83,000	392.4	51.04	2412	757.6	3486	2918	2.961	0.003908	971.1	0.00753
84,000	392.4	48.67	2300	722.5	3032	2906	2.961	0.004098	971.1	0.00786
85,000	392.4	46.47	2198	687.3	2764	2957	2.961	0.004287	971.1	0.00820
86,000	392.4	44.24	2096	657.5	2537	2901	2.961	0.004472	971.1	0.00852
87,000	392.4	42.27	1995	627.5	2317	2807	2.961	0.004653	971.1	0.00894
88,000	392.4	39.41	1895	597.5	2134	2619	2.961	0.004843	971.1	0.0100
89,000	392.4	38.41	1815	570.4	2139	2396	2.961	0.005031	971.1	0.0111
90,000	392.4	36.61	1730	541.6	2186	1734	2.961	0.005247	971.1	0.0125
91,000	392.4	34.92	1650	512.4	2079	1553	2.961	0.005572	971.1	0.0140
92,000	392.4	33.31	1574	494.7	1974	1474	2.961	0.005929	971.1	0.0155
93,000	392.4	31.79	1500	476.9	1892	1395	2.961	0.006284	971.1	0.0171
94,000	392.4	29.89	1426	458.7	1803	1307	2.961	0.006607	971.1	0.0183
95,000	392.4	27.57	1303	409.2	1721	1205	2.961	0.007246	971.1	0.0218
96,000	392.4	25.30	1243	350.5	1637	1188	2.961	0.007929	971.1	0.0254
97,000	392.4	23.19	1188	317.6	1567	1134	2.961	0.008631	971.1	0.0291
98,000	392.4	21.31	1130	285.0	1493	1131	2.961	0.009351	971.1	0.0328
99,000	392.4	20.61	1075	256.6	1424	1079	2.961	0.009745	971.1	0.0363
100,000	392.4	20.61	1075	236.6	1386	1026	2.961	0.01016	971.1	0.0403
101,000	392.4	19.95	1020	220.4	1325	979	2.961	0.01167	971.1	0.0443
102,000	392.4	18.39	969.7	205.4	1276	921.1	2.961	0.01318	971.1	0.0484
103,000	392.4	17.02	917.9	191.6	1234	876.6	2.961	0.01468	971.1	0.0524
104,000	392.4	16.71	867.5	181.1	1193	832.1	2.961	0.01618	971.1	0.0564
105,000	392.4	16.45	820.5	172.5	1153	794.3	2.961	0.01768	971.1	0.0604
106,000	392.4	16.20	774.9	164.1	1113	760.6	2.961	0.01918	971.1	0.0644
107,000	392.4	15.95	734.5	156.7	1073	740.9	2.961	0.02068	971.1	0.0684
108,000	392.4	15.70	694.5	149.3	1033	721.6	2.961	0.02218	971.1	0.0724
109,000	392.4	15.45	659.5	142.9	993	699.9	2.961	0.02368	971.1	0.0764
110,000	392.4	15.20	626.5	136.5	953	679.2	2.961	0.02518	971.1	0.0804
111,000	392.4	14.95	593.5	130.1	913	659.5	2.961	0.02668	971.1	0.0844
112,000	392.4	14.70	562.5	123.7	873	639.8	2.961	0.02818	971.1	0.0884
113,000	392.4	14.45	532.5	117.3	833	620.1	2.961	0.02968	971.1	0.0924
114,000	392.4	14.20	503.5	111.9	793	600.4	2.961	0.03118	971.1	0.0964
115,000	392.4	13.95	475.5	106.5	753	580.7	2.961	0.03268	971.1	0.1004
116,000	392.4	13.70	448.5	101.1	713	561.0	2.961	0.03418	971.1	0.1044
117,000	392.4	13.45	422.5	95.7	673	542.3	2.961	0.03568	971.1	0.1084
118,000	392.4	13.20	397.5	90.3	633	523.6	2.961	0.03718	971.1	0.1124
119,000	392.4	12.95	373.5	85.9	593	504.9	2.961	0.03868	971.1	0.1164
120,000	392.4	12.70	350.5	81.5	553	486.2	2.961	0.04018	971.1	0.1204
122,000	392.4	12.05	297.5	72.4	493	426.5	2.961	0.04368	971.1	0.1334
124,000	392.4	11.40	257.5	63.3	433	366.8	2.961	0.04718	971.1	0.1474
126,000	392.4	10.75	228.5	54.2	373	307.1	2.961	0.05068	971.1	0.1614
128,000	392.4	10.10	201.5	45.1	313	247.4	2.961	0.05418	971.1	0.1754
130,000	392.4	9.45	176.5	36.0	253	187.7	2.961	0.05768	971.1	0.1894
132,000	392.4	8.80	153.5	27.9	193	128.0	2.961	0.06118	971.1	0.2034
134,000	392.4	8.15	132.5	19.8	133	68.3	2.961	0.06468	971.1	0.2174
136,000	392.4	7.50	113.5	11.7	73	10.6	2.961	0.06818	971.1	0.2314
138,000	392.4	6.85	95.5	3.6	17	3.41	2.961	0.1944	1225	0.2454
140,000	392.4	6.20	80.5	1.6	1	1.32	2.961	0.2384	1225	0.2594
142,000	392.4	5.55	67.5	0.6	0	0.33	2.961	0.2824	1225	0.2734
144,000	392.4	4.90	55.5	0	0	0	2.961	0.3264	1225	0.2874
146,000	392.4	4.25	44.5	0	0	0	2.961	0.3704	1225	0.3014
148,000	392.4	3.60	34.5	0	0	0	2.961	0.4144	1225	0.3154
150,000	392.4	2.95	25.5	0	0	0	2.961	0.4584	1225	0.3294
152,000	392.4	2.30	17.5	0	0	0	2.961	0.5024	1225	0.3434
154,000	392.4	1.65	10.5	0	0	0	2.961	0.5464	1225	0.3574
156,000	392.4	1.00	4.5	0	0	0	2.961	0.5904	1225	0.3714
158,000	392.4	0.35	0	0	0	0	2.961	0.6344	1225	0.3854
160,000	392.4	0.35	0	0	0	0	2.961	0.6784	1225	0.4004
162,000	392.4	0.35	0	0	0	0	2.961	0.7224	1225	0.4144
164,000	392.4	0.35	0	0	0	0	2.961	0.7664	1225	0.4284
166,000	392.4	0.35	0	0	0	0	2.961	0.8104	1225	0.4424
168,000	392.4	0.35	0	0	0	0	2.961	0.8544	1225	0.4564
170,000	392.4	0.35	0	0	0	0	2.961	0.8984	1225	0.4704
172,000	392.4	0.35	0	0	0	0	2.961	0.9424	1225	0.4844
174,000	392.4	0.35	0	0	0	0	2.961	0.9864	1225	0.4984
176,000	392.4	0.35	0	0	0	0	2.961	1.0304	1225	0.5124
178,000	392.4	0.35	0	0	0	0	2.961	1.0744	1225	0.5264
180,000	392.4	0.35	0	0	0	0	2.961	1.1184	1225	0.5404
182,000	392.4	0.35	0	0	0	0	2.961	1.1624	1225	0.5544
184,000	392.4	0.35	0	0	0	0	2.961	1.2064	1225	0.5684
186,000	392.4	0.35	0	0	0	0	2.961	1.2504	1225	0.5824
188,000	392.4	0.35	0	0	0	0	2.961	1.2944	1225	0.5964
190,000	392.4	0.35	0	0	0	0	2.961	1.3384	1225	0.6104
192,000	392.4	0.35	0	0	0	0	2.961	1.3824	1225	0.6244
194,000	392.4	0.35	0	0	0	0	2.961	1.4264	1225	0.6384
196,000	392.4	0.35	0	0	0	0	2.961	1.4704	1225	0.6524
198,000	392.4	0.35	0	0	0	0	2.961	1.5144	1225</	

TABLE V -- PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN
INVERSE SQUARE VARIATION OF GRAVITATIONAL FORCE — BRITISH ENGINEERING SYSTEM — Continued

Altitude, h (ft)	Absolute tempera- ture, T (°F abs.)	Pressure, P (lb/ft ²)	Pressure ratio, P/P ₀	Density, ρ (slugs/ft ³)	Density ratio, σ = ρ/ρ ₀	Specific weight, γ = gρ (lb/ft ³)	Coefficient of viscosity, μ = μ ₀ P (lb-sec/ft ²) (1)	Kinematic viscosity, ν = μ/P (ft ² /sec) (1)	Speed of sound, a (ft/sec)	Mean free path of molecules, λ (ft)
(b) For day only										
262,467	432.0	0.07527	3.557×10 ⁻⁵	101.5×10 ⁻⁹	4.268×10 ⁻⁵	3.185×10 ⁻⁶	3.212×10 ⁻⁷	3.165	1019	5.53×10 ⁻³
264,000	432.0	0.07056	3.334	94.56	3.981	2.970	3.212	3.392	1022	5.90
266,000	432.0	0.06484	3.064	86.46	3.636	2.712	3.212	3.715	1026	6.42
268,000	432.0	0.05968	2.820	79.07	3.345	2.480	3.212	4.062	1030	6.97
270,000	432.0	0.05494	2.596	72.34	3.042	2.268	3.212	4.440	1034	7.57
272,000	432.0	0.05060	2.391	65.20	2.784	2.076	3.212	4.852	1038	8.22
272,309	432.0	0.04996	2.361	65.32	2.747	2.048	3.212	4.917	1038	8.32
274,000	432.0	0.04664	2.204	60.18	2.541	1.887	3.232	5.371	1046	8.96
276,000	432.0	0.04302	2.033	54.87	2.299	1.713	3.257	5.958	1051	9.82
278,000	432.0	0.03972	1.877	49.72	2.091	1.558	3.282	6.601	1063	10.7
280,000	447.4	0.03678	1.738	45.35	1.907	1.421	3.306	7.290	1072	11.7
282,000	451.4	0.03409	1.611	41.42	1.742	1.297	3.331	8.042	1081	12.7
284,000	455.4	0.03160	1.493	37.51	1.590	1.184	3.355	8.873	1089	13.9
286,000	459.4	0.02933	1.386	34.60	1.455	1.083	3.379	9.766	1098	15.1
288,000	463.4	0.02726	1.288	31.67	1.332	0.9915	3.403	10.75	1107	16.3
290,000	467.4	0.02537	1.199	29.06	1.222	0.9095	3.427	11.79	1116	17.7
292,000	471.4	0.02362	1.116	26.66	1.121	0.8342	3.451	12.94	1124	19.2
294,000	475.4	0.02201	1.048	24.49	1.030	0.7663	3.475	14.19	1133	20.7
296,000	479.4	0.02055	0.9710	22.55	0.9484	0.7054	3.499	15.52	1142	22.4
298,000	483.4	0.01919	0.9069	20.77	0.8734	0.6495	3.522	16.96	1151	24.2
300,000	487.4	0.01794	0.8479	19.15	0.8053	0.5988	3.546	18.52	1160	26.1
302,000	491.4	0.01679	0.7933	17.67	0.7430	0.5524	3.569	20.20	1168	28.1
304,000	495.4	0.01573	0.7435	16.33	0.6869	0.5105	3.592	22.00	1177	30.2
306,000	499.4	0.01475	0.6970	15.10	0.6352	0.4720	3.616	23.95	1186	32.5
308,000	503.4	0.01383	0.6537	13.97	0.5877	0.4366	3.639	26.05	1195	34.9
310,000	507.4	0.01299	0.6140	12.95	0.5446	0.4046	3.662	28.28	1204	37.4
312,000	511.5	0.01221	0.5772	12.01	0.5051	0.3751	3.685	30.68	1213	40.1
314,000	515.5	0.01149	0.5431	11.15	0.4690	0.3482	3.708	33.26	1222	43.0
316,000	519.5	0.01082	0.5114	10.37	0.4359	0.3236	3.731	35.98	1231	46.0
318,000	523.5	0.01020	0.4819	9.640	0.4054	0.3009	3.754	38.94	1240	49.2
320,000	527.5	0.009620	0.4446	8.977	0.3775	0.2802	3.777	42.07	1248	52.5
322,000	531.5	0.008079	0.4290	8.361	0.3516	0.2609	3.799	45.44	1257	56.1
324,000	535.5	0.006979	0.4054	7.800	0.3280	0.2424	3.822	49.00	1265	59.8
326,000	539.5	0.0080303	0.3829	7.274	0.3059	0.2269	3.844	52.85	1275	63.7
328,000	543.5	0.007663	0.3621	6.791	0.2856	0.2118	3.867	56.94	1284	67.9
328,083	543.6	0.007568	0.3614	6.775	0.2849	0.2113	3.887	57.08	1285	68.0
330,000	547.5	0.007248	0.3425	6.375	0.2681	0.1988	3.889	61.00	1289	72.3
332,000	551.5	0.006867	0.3245	5.997	0.2522	0.1871	3.911	65.22	1294	76.8
334,000	555.5	0.006505	0.3074	5.640	0.2372	0.1758	3.933	69.73	1298	81.7
336,000	559.5	0.006167	0.2914	5.307	0.2232	0.1654	3.955	74.52	1303	86.8
338,000	563.5	0.005843	0.2761	4.994	0.2100	0.1556	3.977	79.64	1308	92.2
340,000	567.5	0.005540	0.2618	4.701	0.1977	0.1464	3.999	85.07	1312	97.9
342,000	571.5	0.005257	0.2484	4.430	0.1863	0.1379	4.021	90.77	1317	104
344,000	575.5	0.004992	0.2356	4.178	0.1757	0.1301	4.043	96.77	1322	110
346,000	579.5	0.004736	0.2236	3.935	0.1625	0.1226	4.065	103.3	1326	117
348,000	583.5	0.004499	0.2126	3.714	0.1562	0.1156	4.086	110.0	1331	124
350,000	587.5	0.004275	0.2020	3.505	0.1474	0.1091	4.108	117.2	1335	131
352,000	591.5	0.004061	0.1919	3.305	0.1390	0.1029	4.129	124.9	1340	139
354,000	595.5	0.003860	0.1824	3.122	0.1313	0.09716	4.151	133.0	1344	147
356,000	599.5	0.003672	0.1735	2.949	0.1240	0.09173	4.172	141.5	1349	156
358,000	603.5	0.003494	0.1651	2.787	0.1172	0.08668	4.193	150.4	1353	165
360,000	607.5	0.003329	0.1573	2.637	0.1110	0.08205	4.214	159.8	1358	174
362,000	611.5	0.003168	0.1497	2.494	0.1049	0.07753	4.236	169.8	1362	184
364,000	615.5	0.003016	0.1425	2.359	0.09922	0.07333	4.257	180.4	1367	195
366,000	619.5	0.002874	0.1358	2.253	0.09395	0.06942	4.278	191.5	1371	206
368,000	623.5	0.002738	0.1294	2.115	0.08894	0.06571	4.299	203.3	1376	217
370,000	627.5	0.002611	0.1234	2.004	0.08428	0.06225	4.319	215.6	1380	229
372,000	631.5	0.002489	0.1176	1.898	0.07981	0.05824	4.340	228.7	1384	242
374,000	635.5	0.002374	0.1122	1.799	0.07566	0.05568	4.361	242.4	1389	255
376,000	639.5	0.002266	0.1071	1.707	0.07177	0.05298	4.382	256.7	1393	263
378,000	643.5	0.002163	0.1022	1.618	0.06806	0.05023	4.402	272.1	1398	263
380,000	647.5	0.002054	0.09754	1.535	0.06456	0.04764	4.423	288.1	1402	299
382,000	651.5	0.001971	0.09316	1.457	0.06128	0.04522	4.443	304.9	1406	315
384,000	655.5	0.001884	0.08901	1.384	0.05819	0.04293	4.464	322.5	1411	331
386,000	659.5	0.001800	0.08505	1.314	0.05527	0.04076	4.484	341.2	1415	349
388,000	663.5	0.001721	0.08131	1.249	0.05252	0.03873	4.504	360.6	1419	367
390,000	667.5	0.001656	0.07776	1.187	0.04992	0.03681	4.525	381.2	1423	386
392,000	671.5	0.001573	0.07434	1.128	0.04744	0.03497	4.545	402.9	1428	406
393,700	675.0	0.001515	0.07160	1.081	0.04546	0.033350	4.562	422.0	1431	424

¹The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE V.— PROPERTIES OF THE UPPER ATMOSPHERE FOR TENTATIVE STANDARD TEMPERATURES BASED ON AN
INVERSE SQUARE VARIATION OF GRAVITATIONAL FORCE— BRITISH ENGINEERING SYSTEM — Concluded

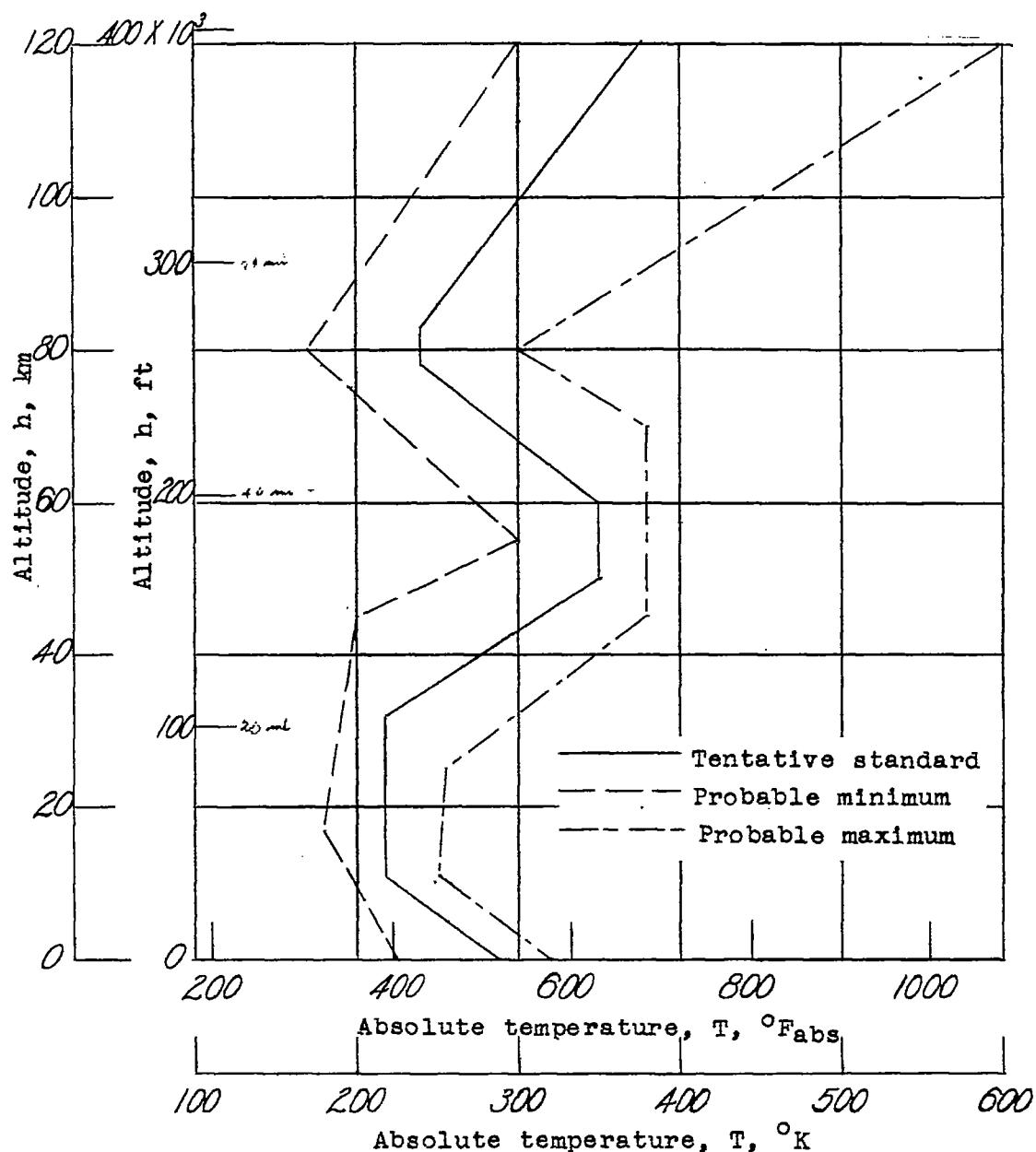
Altitude, h (ft)	Absolute tempera- ture, T (°F abs.)	Pressure, P (lb/ft ²)	Pressure ratio, P/P ₀	Density, ρ (slugs/ft ³)	Density ratio, ρ = ρ/P ₀	Specific weight, w = gρ (lb/ft ³)	Coefficient of viscosity μ = μ ₀ P ₀ (lb-sec/ft ²) (l)	Kinematic viscosity, U = μ (ft ² /sec) (1)	Speed of sound, a (ft/sec)	Mean free path of molecules, λ (ft)
(e) For night only										
262,467	432.0	0.07527	3.557×10 ⁻⁵	101.5×10 ⁻⁹	4.268×10 ⁻⁵	3.185×10 ⁻⁶	3.212×10 ⁻⁷	3.165	1019	5.53×10 ⁻³
264,000	432.0	0.07051	3.332	95.07	3.998	2.983	3.212	3.379	1019	2.28
266,000	432.0	0.06580	3.062	87.36	3.674	2.741	3.212	3.677	1019	6.42
268,000	432.0	0.06055	2.814	80.30	3.377	2.519	3.212	4.000	1019	6.98
270,000	432.0	0.05473	2.586	73.79	3.103	2.314	3.212	4.353	1019	7.60
272,000	432.0	0.05032	2.378	67.87	2.854	2.128	3.212	4.732	1019	8.26
272,309	432.0	0.04905	2.346	66.04	2.815	2.099	3.212	4.798	1019	8.37
274,000	435.4	0.04622	2.184	67.83	2.600	1.938	3.232	5.227	1023	9.06
276,000	439.4	0.04252	2.009	56.36	2.370	1.766	3.257	5.779	1028	9.94
278,000	443.4	0.03913	1.849	51.41	2.162	1.611	3.282	6.384	1032	10.9
280,000	447.4	0.03604	1.703	46.92	1.973	1.470	3.306	7.046	1037	11.9
282,000	451.4	0.03320	1.569	42.85	1.802	1.342	3.331	7.774	1042	13.1
284,000	455.4	0.03056	1.449	39.21	1.649	1.228	3.355	8.551	1046	14.3
286,000	459.4	0.02832	1.338	35.91	1.510	1.124	3.379	9.401	1051	15.8
288,000	463.4	0.02618	1.237	32.91	1.384	1.030	3.403	10.34	1055	17.0
290,000	467.4	0.02423	1.145	30.20	1.270	0.9452	3.427	11.35	1060	18.5
292,000	471.4	0.02239	1.058	27.65	1.163	0.8654	3.451	12.48	1064	20.2
294,000	475.4	0.02072	0.9793	25.40	1.068	0.7949	3.475	13.68	1069	22.0
296,000	479.4	0.01939	0.8869	23.32	0.9806	0.7294	3.499	15.00	1073	24.0
298,000	483.4	0.01780	0.8409	21.44	0.9017	0.6706	3.523	16.43	1078	26.1
300,000	487.4	0.01653	0.7810	19.75	0.8306	0.6176	3.546	17.95	1082	28.3
302,000	491.4	0.01554	0.7247	18.18	0.7645	0.5683	3.569	19.63	1087	30.8
304,000	495.4	0.01424	0.6729	16.74	0.7041	0.5233	3.593	21.46	1091	33.4
306,000	499.4	0.01324	0.6255	15.44	0.6492	0.4824	3.618	23.42	1096	35.2
308,000	503.4	0.01231	0.5818	14.25	0.5991	0.4451	3.639	25.54	1100	39.2
310,000	507.4	0.01165	0.5514	13.15	0.5531	0.4109	3.662	27.84	1104	42.4
312,000	511.5	0.01067	0.5042	12.15	0.5110	0.3792	3.685	30.33	1109	46.0
314,000	515.5	0.00994	0.4597	11.23	0.4724	0.3508	3.708	33.02	1113	49.7
316,000	519.5	0.009265	0.4378	10.39	0.4369	0.3244	3.731	35.91	1117	53.7
318,000	523.5	0.008643	0.4084	9.616	0.4044	0.3002	3.754	39.04	1122	58.0
320,000	527.5	0.008061	0.3809	8.903	0.3744	0.2779	3.777	42.42	1126	62.7
322,000	531.5	0.007527	0.3557	8.251	0.3470	0.2575	3.799	46.04	1130	67.6
324,000	535.5	0.007028	0.3321	7.645	0.3215	0.2385	3.822	49.99	1134	73.0
326,000	539.5	0.006573	0.3105	7.096	0.2984	0.2213	3.844	51.17	1139	78.6
328,000	543.5	0.006146	0.2904	6.587	0.2770	0.2054	3.867	58.71	1143	84.6
330,000	547.5	0.005750	0.2717	6.118	0.2573	0.1908	3.889	63.57	1147	91.1
332,000	551.5	0.005379	0.2542	5.681	0.2389	0.1771	3.911	68.84	1151	98.1
334,000	555.5	0.005039	0.2381	5.284	0.2222	0.1647	3.933	74.43	1155	105
336,000	559.5	0.004721	0.2231	4.915	0.2067	0.1532	3.955	80.47	1160	113
338,000	563.5	0.004427	0.2092	4.577	0.1925	0.1426	3.977	86.91	1164	122
340,000	567.5	0.004152	0.1962	4.261	0.1792	0.1327	3.999	93.85	1168	131
342,000	571.5	0.003892	0.1839	3.966	0.1668	0.1235	4.021	101.4	1172	140
344,000	575.5	0.003655	0.1727	3.700	0.1556	0.1152	4.043	109.3	1176	150
344,487	576.5	0.003602	0.1702	3.638	0.1530	0.1134	4.048	111.2	1177	153
346,000	579.5	0.003433	0.1563	3.429	0.1442	0.1058	4.065	118.5	1185	161
348,000	583.5	0.003231	0.1582	3.172	0.1337	0.09896	4.108	139.5	1205	184
350,000	587.5	0.003041	0.1437	2.946	0.1239	0.09269	4.108	151.1	1215	197
352,000	591.5	0.002863	0.1353	2.732	0.1149	0.08902	4.129	163.6	1226	211
354,000	595.5	0.002700	0.1276	2.537	0.1067	0.07893	4.151	176.9	1236	225
356,000	599.5	0.002546	0.1203	2.358	0.09916	0.07334	4.172	191.1	1246	240
358,000	603.5	0.002404	0.1136	2.194	0.09227	0.06923	4.193	192.0	1249	233
360,000	607.5	0.002273	0.1074	2.044	0.08597	0.06356	4.214	206.2	1256	255
362,000	611.2	0.002150	0.1016	1.906	0.08015	0.05925	4.236	222.2	1266	271
364,000	615.2	0.002038	0.09614	1.778	0.07476	0.05525	4.257	239.4	1277	288
366,000	619.0	0.001928	0.09111	1.661	0.06984	0.05161	4.278	257.6	1287	306
368,000	623.6	0.001828	0.08639	1.553	0.06529	0.04824	4.299	276.8	1297	325
370,000	627.6	0.001736	0.08201	1.453	0.06111	0.04514	4.319	297.2	1308	345
372,000	631.6	0.001649	0.07790	1.361	0.05724	0.04227	4.340	318.9	1318	365
374,000	635.6	0.001567	0.07405	1.276	0.05366	0.03962	4.361	341.8	1328	386
376,000	639.6	0.001489	0.07038	1.197	0.05033	0.03716	4.382	366.1	1339	409
378,000	643.6	0.001417	0.06698	1.123	0.04722	0.03485	4.402	392.0	1349	433
380,000	647.6	0.001350	0.06379	1.055	0.04436	0.03274	4.423	419.2	1360	457
382,000	651.6	0.001286	0.06079	0.9916	0.04170	0.03077	4.443	448.0	1370	482
384,000	655.6	0.001227	0.05797	0.9331	0.03924	0.02895	4.464	478.4	1381	509
386,000	659.6	0.001170	0.05531	0.8764	0.03694	0.02725	4.484	510.5	1391	536
388,000	663.6	0.001118	0.05282	0.8277	0.03481	0.02567	4.504	544.2	1401	565
390,000	667.6	0.001068	0.04945	0.7804	0.03282	0.02420	4.525	579.8	1412	595
392,000	671.6	0.001020	0.04623	0.7364	0.03097	0.02282	4.545	617.2	1422	626
393,700	675.0	0.0009830	0.04645	0.7015	0.02950	0.02173	4.562	650.4	1431	653

¹The values for viscosity listed in these columns are not applicable at the higher altitudes where the mean free paths of the molecules are comparable to or longer than the dimensions of the body being considered. Furthermore, the values listed are based on the conventional Sutherland formula for normal air and, consequently, no allowance has been made for the effect of dissociated oxygen in the atmosphere at the higher levels.

TABLE VI.— LATITUDE CORRECTION FACTORS FOR VALUES OF PRESSURE IN TABLES IV AND V

Latitude, deg		0	10	20	30	40	50	60	70	80	90
Altitude, h (km)	(ft)										
(a) For both day and night											
20	65,617	1.0078	1.0073	1.0060	1.0039	1.0014	0.9988	0.9963	0.9943	0.9929	0.9925
30	98,425	1.0120	1.0112	1.0092	1.0060	1.0022	.9981	.9943	.9912	.9892	.9885
40	131,233	1.0158	1.0148	1.0121	1.0080	1.0029	.9975	.9925	.9884	.9858	.9848
50	164,042	1.0187	1.0176	1.0144	1.0094	1.0034	.9971	.9911	.9863	.9832	.9821
60	196,850	1.0213	1.0200	1.0164	1.0108	1.0039	.9967	.9899	.9844	.9808	.9796
70	229,658	1.0242	1.0227	1.0186	1.0122	1.0044	.9962	.9866	.9824	.9783	.9769
80	262,467	1.0278	1.0260	1.0212	1.0140	1.0051	.9957	.9869	.9798	.9752	.9736
(b) For day only											
80	262,467	1.0278	1.0260	1.0212	1.0140	1.0051	0.9957	0.9869	0.9798	0.9752	0.9736
90	295,275	1.0312	1.0293	1.0239	1.0157	1.0057	.9952	.9853	.9774	.9722	.9704
100	328,083	1.0340	1.0319	1.0261	1.0171	1.0062	.9947	.9840	.9754	.9698	.9679
110	360,892	1.0364	1.0342	1.0279	1.0193	1.0066	.9944	.9830	.9738	.9678	.9657
120	393,700	1.0385	1.0361	1.0295	1.0193	1.0070	.9940	.9820	.9723	.9660	.9638
(c) For night only											
80	262,467	1.0278	1.0260	1.0212	1.0140	1.0051	0.9957	0.9869	0.9798	0.9752	0.9736
90	295,275	1.0314	1.0295	1.0241	1.0158	1.0057	.9951	.9852	.9772	.9721	.9703
100	328,083	1.0346	1.0325	1.0265	1.0174	1.0063	.9946	.9838	.9750	.9693	.9673
110	360,892	1.0374	1.0352	1.0287	1.0188	1.0068	.9942	.9825	.9730	.9669	.9647
120	393,700	1.0397	1.0373	1.0304	1.0199	1.0072	.9938	.9815	.9714	.9649	.9627

 NATIONAL ADVISORY
 COMMITTEE FOR AERONAUTICS



NATIONAL ADVISORY
COMMITTEE FOR AERONAUTICS

Figure 1.- Variation of ambient temperature with altitude.

FIG. 2

NACA TN NO. 1200

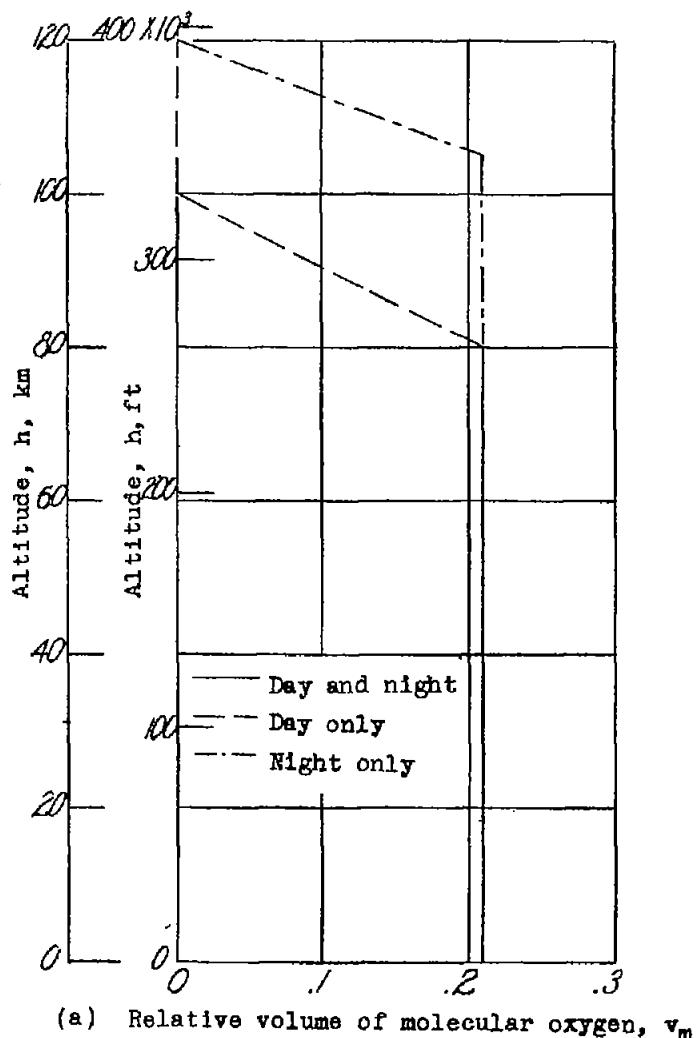
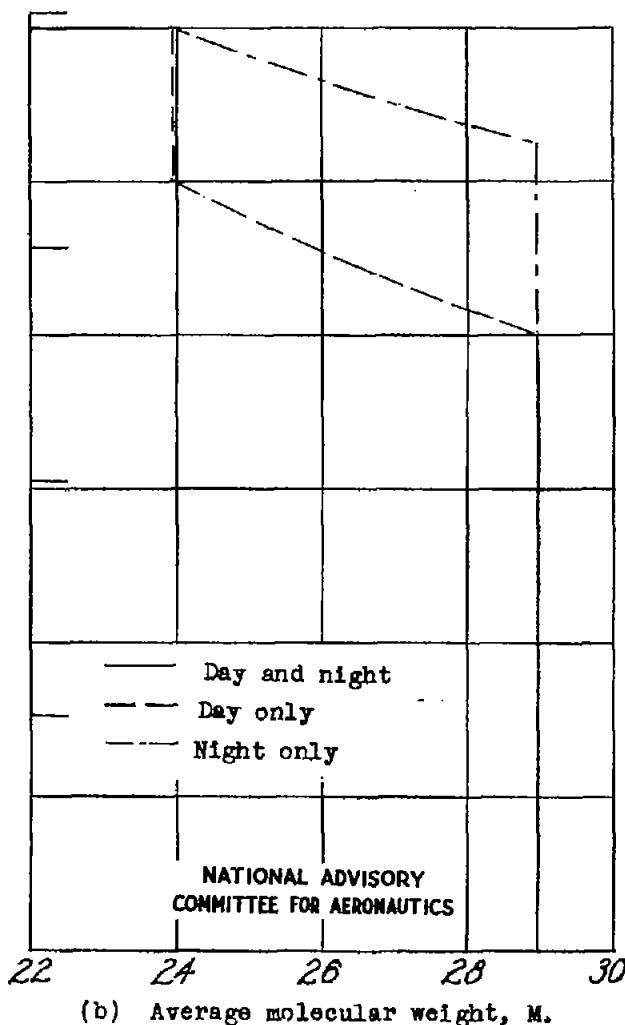
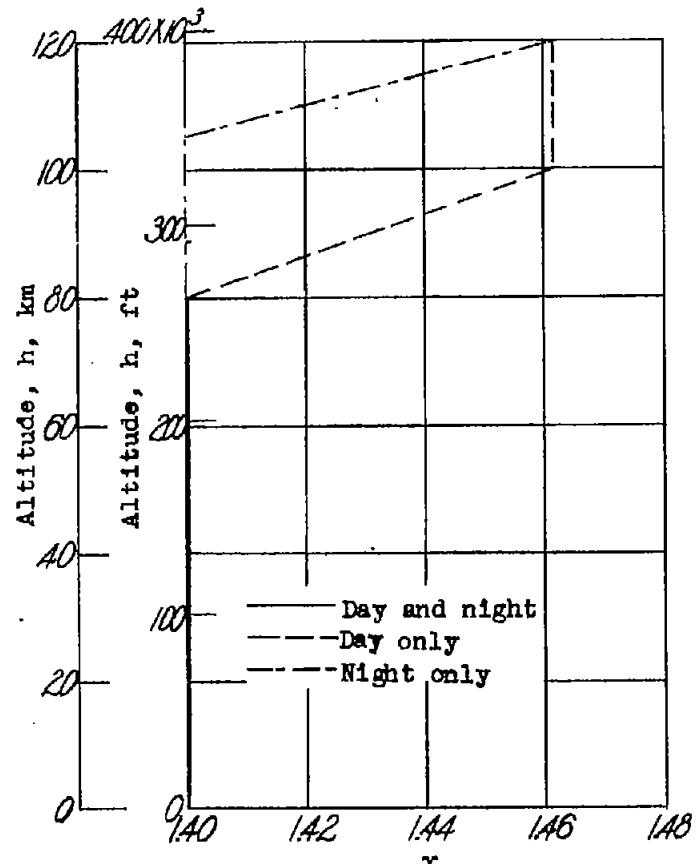
(a) Relative volume of molecular oxygen, v_m .(b) Average molecular weight, M .

Figure 2.- Variation of composition of the tentative standard atmosphere with altitude. (The dissociation of oxygen is the only change in composition occurring in the tentative standard atmosphere.)

Fig. 3a,b



NATIONAL ADVISORY
COMMITTEE FOR AERONAUTICS.

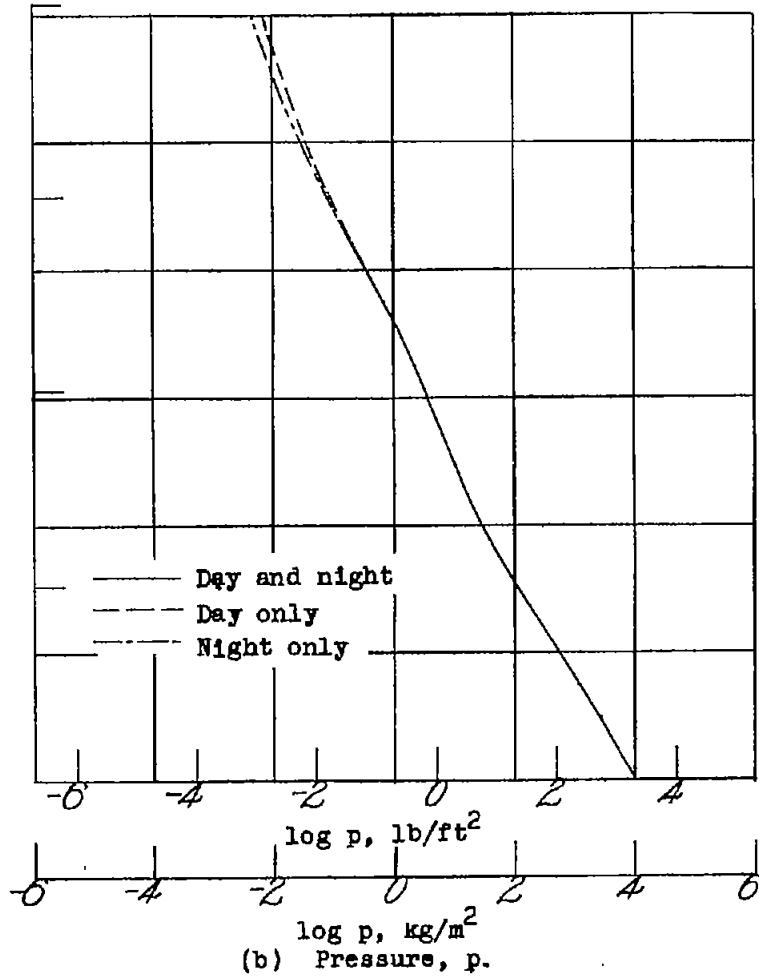
(a) Ratio of specific heats, γ .(b) Pressure, p .

Figure 3. Variation with altitude of the physical properties of the tentative standard atmosphere.

FIG. 3c,d

NACA TN No. 1200

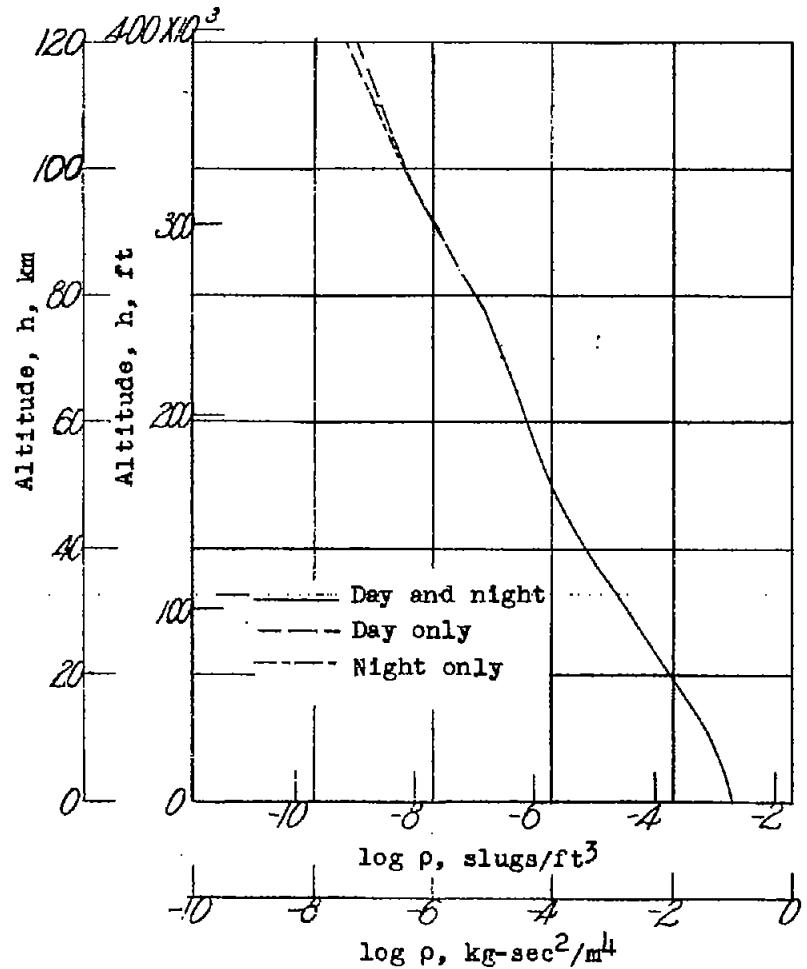
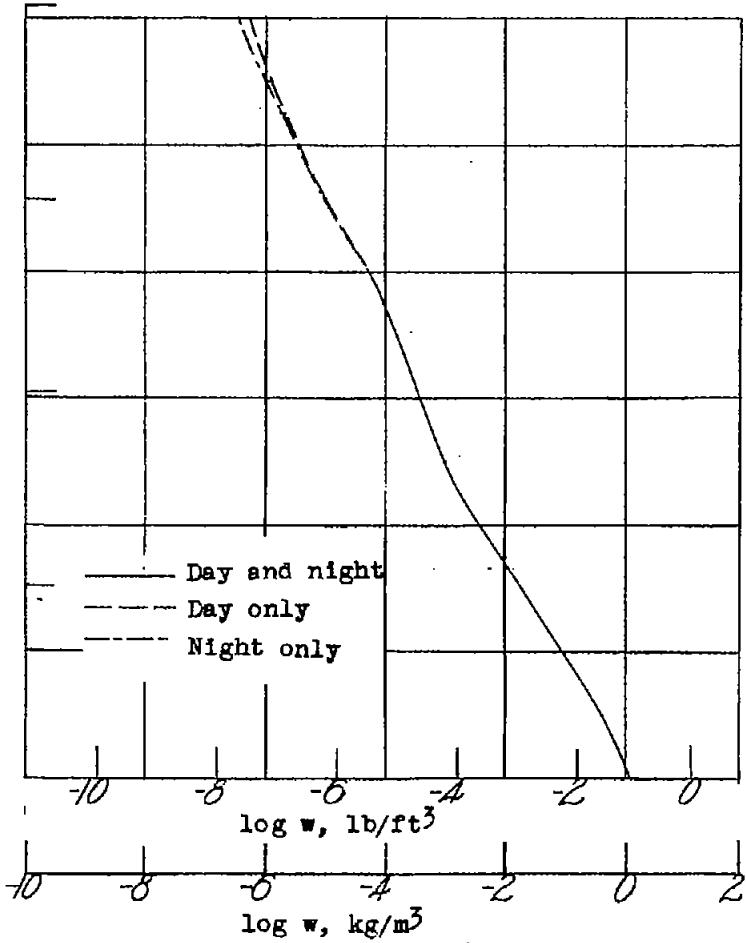
(c) Density, ρ .(d) Specific weight, w .

Figure 3.- Continued.

NATIONAL ADVISORY
COMMITTEE FOR AERONAUTICS.

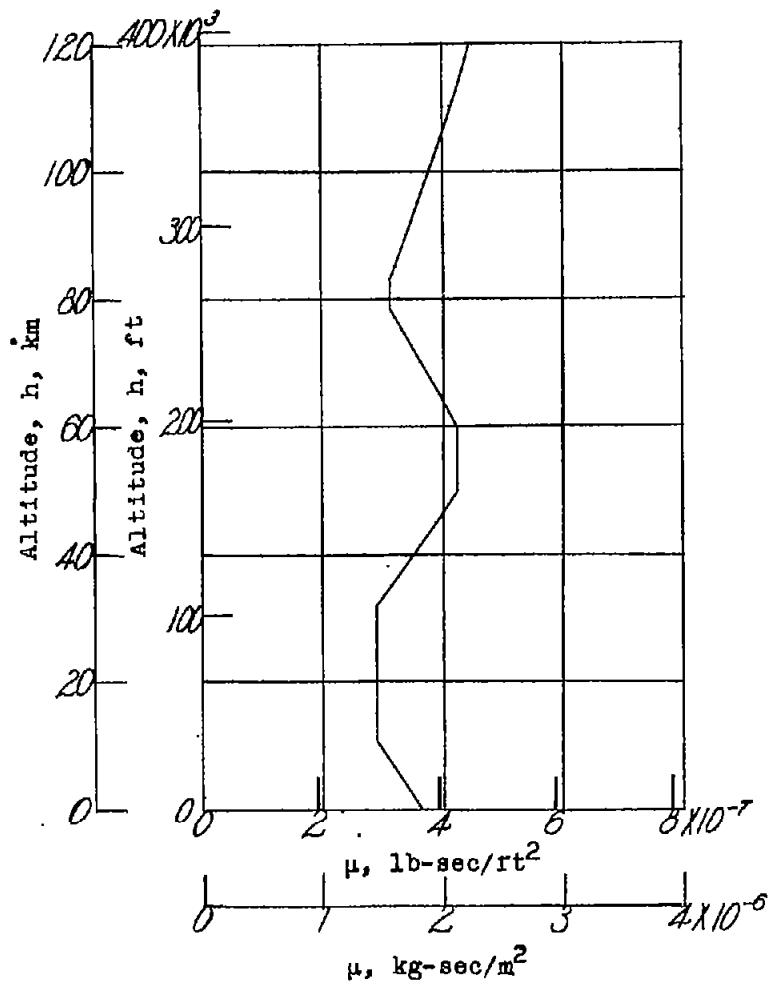
(e) Coefficient of viscosity, μ .

Figure 3.- Continued.

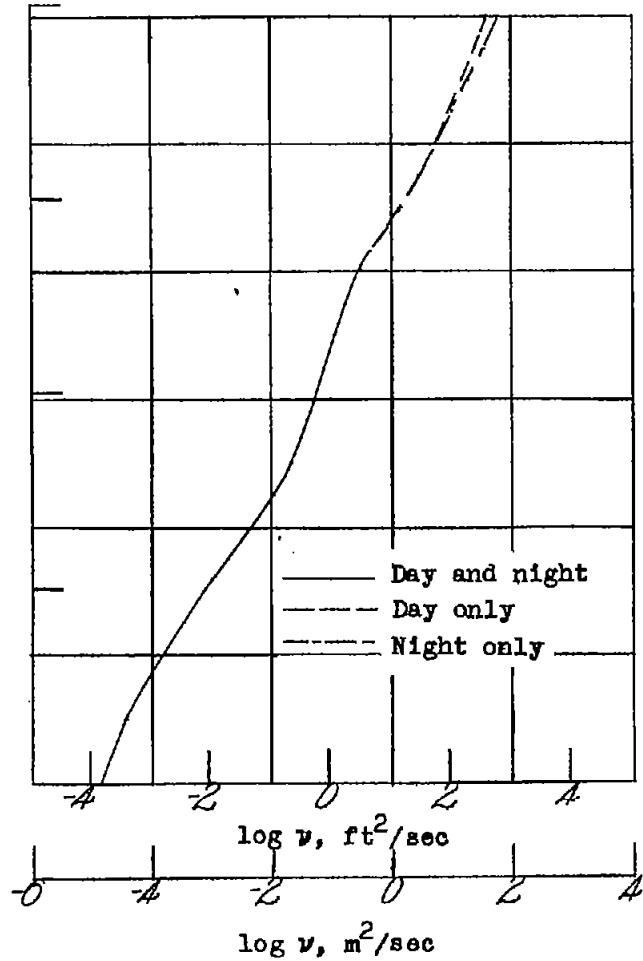
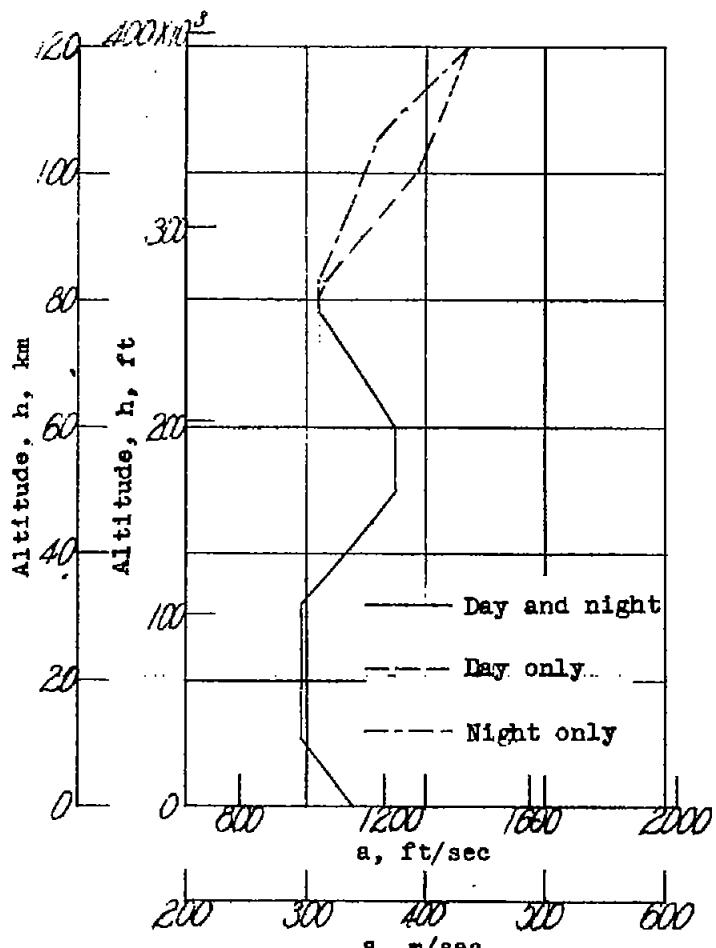
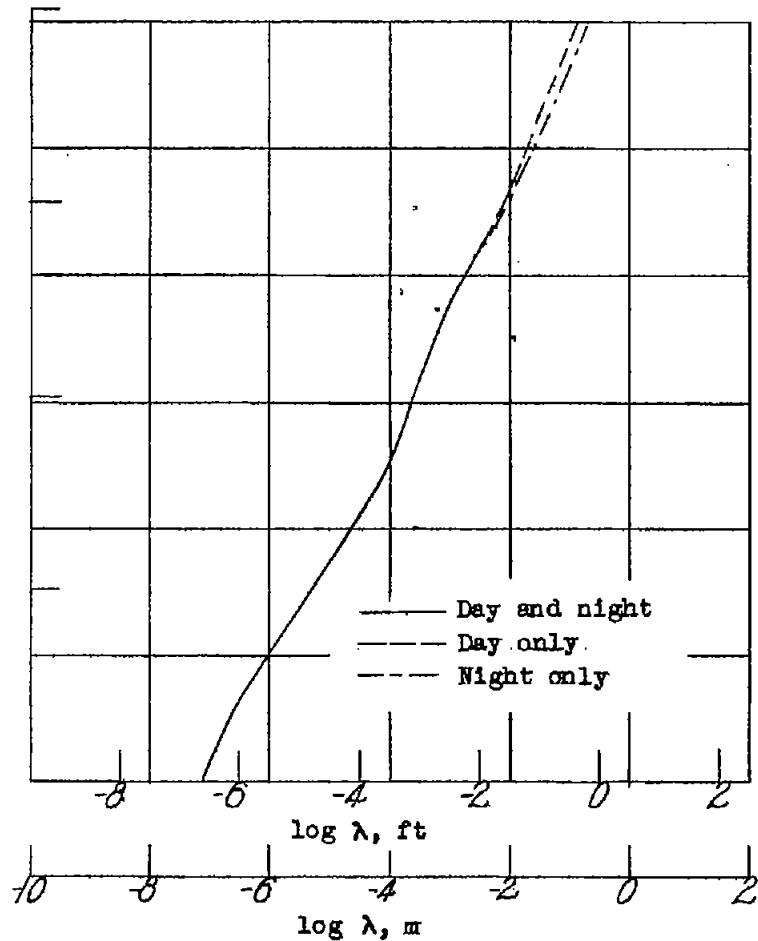
NATIONAL ADVISORY
COMMITTEE FOR AERONAUTICS.(f) Kinematic viscosity, ν .

FIG. 3g,h

NACA TN No. 1200



(g) Speed of sound, a .



(h) Mean free path of molecules, λ .

Figure 3.- Concluded.

NATIONAL ADVISORY
COMMITTEE FOR AERONAUTICS.